

# Conjecture involving repunits, repdigits, repnumbers and also the primes of the form $30k+11$ and $30k+13$

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**Abstract.** In my previous paper "Conjecture on semiprimes  $n = p \cdot q$  related to the number of primes up to  $n$ " I was wondering if there exist a class of numbers  $n$  for which the number of primes up to  $n$  of the form  $30k + 1$ ,  $30k + 7$ ,  $30k + 11$ ,  $30k + 13$ ,  $30k + 17$ ,  $30k + 19$ ,  $30k + 23$  and  $30k + 29$  is equal in each of these eight sets. I didn't yet find such a class, but I observed that around the repdigits, repunits and repnumbers (numbers obtained concatenating not the unit or a digit but a number) the distribution of primes in these eight sets tends to draw closer and I made a conjecture about it.

## Conjecture:

There exist an infinity of repnumbers  $n$  (repunits, repdigits and numbers obtained concatenating not the unit or a digit but a number) for which the number of primes up to  $n$  of the form  $30k + 11$  is equal to the number of primes up to  $n$  of the form  $30k + 13$ .

### The sequence of these repnumbers $n$ :

(in the bracket is the number of primes up to  $n$ , equally for each of the two sets)

: 22 (1), 33 (1), 44 (2), 55 (2), 66 (2), 77 (3), 88 (3),  
99 (3), 111 (4), 222 (6), 333 (9), 444 (11), 666 (15),  
777 (17), 1818 (36), 2020 (39), 2828 (52), 2929 (53)...

### Few larger such repnumbers $n$ :

: 11111, because we have up to  $n$  :  
: 167 primes of the form  $30k + 11$ ;  
: 167 primes of the form  $30k + 13$ ;  
  
: 888888, because we have up to  $n$  :  
: 8816 primes of the form  $30k + 11$ ;  
: 8816 primes of the form  $30k + 13$ ;  
  
: 11111111, because we have up to  $n$  :  
: 91687 primes of the form  $30k + 11$ ;  
: 91687 primes of the form  $30k + 13$ .