

## Fermat's last theorem

In Memory of my MOTHER

All calculations are done with numbers in base  $n$ , a prime number greater than 2.

The notations:

$A', A'', A''', A_{(t)}$  – the first, the second, the third, the  $t$ -th digit from the end of the number  $A$ ;

$A_{[t]}$  – is the  $k$ -digit ending of the number  $A$  (i.e.  $A_{[t]} = A \bmod n^t$ ).

0°) **Lemma.**

The sum of the numbers  $a_i^n$  (where  $a_i=1, 2, \dots, n-1$ ) ends by  $d00$ , where  $d$  is a digit and  $d=(n-1)/2$ .

### Proof of the first case of the FLT

Let's assume that for co-prime natural numbers  $A, B, C$ , where  $(ABC)' \neq 0$  and  $n$  is a prime number  $n > 2$ ,

1°)  $[D=] A^n + B^n - C^n = 0$ , where, as it is known [see [vixra:1707.0410](https://vixra.org/1707.0410)],

$(A+B-C)_{[2]} = 0$  and  $A'+B'-C'$  is either 0 or  $n-1$ , and therefore the digit

2°)  $u'' = (A''+B''-C'')$  is either 0 (if  $A'+B'-C'=0$ ) or  $n-1$  (if  $A'+B'-C'=n$ ).

3°) If we multiply 1° by  $g^{nm}$ , where  $g=1, 2, \dots, n-1$ , we find  $n-1$  equivalent equations..

Leave in all equations 3° only the last digits, i.e. put  $A=A', B=B', C=C'$ . Then the sum of powers for each of the letters  $A, B, C$ , as well as the total sum of all  $n-1$  of the numbers  $D$  of 3°, has an ending  $d00$  has an ending  $d00$  [where  $d=(n-1)/2$  – see 0°].

In each the equations 3° the digit  $D''' > 0$  [otherwise after the operation 3° with this equality with  $D''' = 0$  the digit  $D'''$  in the total sum is also zero] and there is equality with

4°)  $D''' > 1$  [otherwise, in the total sum of  $n-1$  equals 3°, digit  $D''' \neq (n-1)/2$ ].

However, restoring in the equation 4° digits of  $A'', B'', C''$  cannot convert this digit into 0 because, as it follows from the binomial theorem

5°)  $A^n = (\dots + A''n + A')^n$ ,  $B^n = (\dots + B''n + B')^n$ ,  $C^n = (\dots + C''n + C')^n$

and from the Small Theorem, the third digit in the sum of the penultimate three terms in the binomial decomposition  $-(A^{n-1}A^n+B^{n-1}B^n-C^{n-1}C^n)' [=u^n, \text{ i.e. } 0 \text{ or } n-1, - \text{ see } 3^\circ]$ , where  $A^{n-1}=B^{n-1}=C^{n-1}=1$ , – it is either 0 or  $n-1$  (see  $2^\circ$ ).

Thus, Fermat's equality in the first case is contradictory in the third digit also for two-digit numbers  $A, B, C$ . Well, the third and subsequent digits of the bases  $A, B, C$  do not participate in the formation of the third digits of degrees (see  $5^\circ$ ).

From what follows the truth of FLT in the first case.

### **Proof of the second case of the FLT (A is multiple of n)**

Let's assume that for co-prime natural numbers  $A [=n^k A^\circ]$ ,  $B, C$  and a prime  $n > 2$

- 1°)  $A^n+B^n-C^n=0$  and  $C^n-B^n=(C-B)P$ , where, as it is known [see [viXra:1707.0410](https://arxiv.org/abs/1707.0410)],
- 1.1°)  $(C-B)_{[kn-1]}=0, P=P^\circ n, A^n=n^{kn}A^{\circ n}, U=A+B-C=n^k u$  ( $u' \neq 0, k > 1$ ).
- 1.2°)  $C-A=b^n, B=bq; A+B=c^n, C=cr; q^n=Q, r^n=R, P^\circ=Q'=R'=1$ ;  
the numbers  $A^\circ, P^\circ, n, b, q, c, r$  are co-prime.
- 2°) Consider the number  $D=(A+B)^n-(C-B)^n-(C-A)^n$ , where  $(C-B)_{[k+2]}^n=0$ , from here
- 2.1°)  $D_{[k+2]}=[(A+B)^n-(C-B)^n-(C-A)^n+(A^n+B^n-C^n)]_{[k+2]}=\{[(A+B)^n-C^n]-[(C-A)^n-B^n]\}_{[k+2]}$ , or
- 2.2°)  $D_{[k+2]}=\{[c^n(c^{n-1}-r)V]-[b^n(b^{n-1}-q)W]\}_{[k+2]}$ , where  $c'=b', V_{[2]}=W_{[2]}=10$ ,  
 $(c^{n-1}-r)_{[k]}=(b^{n-1}-q)_{[k]}=0, (c^{n-1}-r)_{(k+1)}=(b^{n-1}-q)_{(k+1)}$  (since  $[(A+B-C)/cn^k]'=[(A+B-C)/bn^k]'$ , where  $c'=b'$ ) and therefore,
- 3°)  $D_{[k+2]}=0$ .
- However after removing parenthesis in Newton's binomials in  $2^\circ$  and grouping the summands having equal powers into pairs, we can notice that all pairs end by  $k+2$  zeroes and only the pair in
- 4°)  $n^{k+1}A^\circ C^{n-1}+n^{k+1}A^\circ B^{n-1}$  ends by  $k+1$  zeroes, because  $(k+2)$ -th digit is equal to  $(2A^\circ)'$  (since the numbers  $C^{n-1}$  and  $B^{n-1}$  end by digit 1 – see SFT), which contradicts to  $3^\circ$ !

Thus FLT is verified.

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