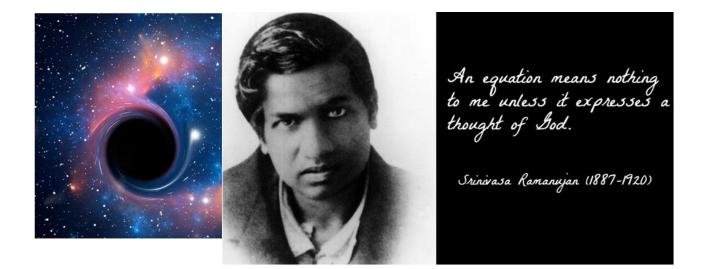
On some Ramanujan's equations: mathematical connections with various equations concerning some sectors of Particle Physics and Black Hole/Wormhole Physics. III

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#### Abstract

In this paper we have described the mathematical connections between various Ramanujan's equations (class invariants) and some expressions of various topics of Particle Physics and Black Hole/Wormhole Physics

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(N.O.A – Pics. from the web)

From:

**Wormholes in generalized hybrid metric-Palatini gravity obeying the matter null energy condition everywhere -** *Joao Luis Rosa, Jose P. S. Lemos, and Francisco S. N. Lobo* - arXiv:1808.08975v1 [gr-qc] 27 Aug 2018,

Now, we have that:

Eq. (19), (20), and (21), we obtain the energy density, the radial pressure, and the tangential pressure as

$$\rho = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( 24 - 31 \frac{r_0^2}{r^2} \right) \,, \tag{42}$$

$$p_r = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( 16 - 13 \frac{r_0^2}{r^2} \right) \,, \tag{43}$$

$$p_t = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( -32 + 39 \frac{r_0^2}{r^2} \right) , \qquad (44)$$

respectively.

From

$$\rho = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( 24 - 31 \frac{r_0^2}{r^2} \right)$$
$$p_r = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( 16 - 13 \frac{r_0^2}{r^2} \right)$$
$$p_t = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( -32 + 39 \frac{r_0^2}{r^2} \right)$$

for

$$\zeta_0 = -10.96$$
,  $r_0 = 2\sqrt{10/11} = 1.90693$   $V_0 = -42$ .

M = 13.12806e+39, r = 1.94973e+13 we obtain:

From the above expressions, we obtain:

$$\rho = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( 24 - 31 \frac{r_0^2}{r^2} \right)$$

((1.94973e+13)^2))))

#### **Input interpretation:**

 $\frac{1.90693^2}{2 \left(1.94973 \times 10^{13}\right)^6 \times (-42) \times 0.006} \left(24 - 31 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^2}\right)$ 

#### **Result:**

 $-3.152124502393692812260221722005958164890727218390153...\times 10^{-78}$ -3.15212450239369...\*10<sup>-78</sup>

$$p_r = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( 16 - 13 \frac{r_0^2}{r^2} \right)$$

 $(1.90693^{2}) / (((2*(1.94973e+13)^{6}*(-42)*0.006))) * (((16-13*(1.90693^{2})/(1.90693^{2})))))) * (((16-13*(1.90693^{2})/(1.90693^{2}))))))))$ ((1.94973e+13)^2))))

 $\frac{1.90693^2}{2 \left(1.94973 \times 10^{13}\right)^6 \times (-42) \times 0.006} \left(16 - 13 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^2}\right)$ 

#### **Result:**

 $-2.101416334929128541506814490969367158531995710971960...\times10^{-78}$  $-2.10141633492912854...*10^{-78}$ 

$$p_t = \frac{r_0^2}{2r^6 V_0 \kappa^2} \left( -32 + 39 \frac{r_0^2}{r^2} \right)$$

((1.94973e+13)^2))))

 $\frac{1.90693^2}{2(1.94973 \times 10^{13})^6 \times (-42) \times 0.006} \left(-32 + 39 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^2}\right)$ 

#### **Result:**

 $\begin{array}{l} 4.2028326698582570830136289656061079302992555502151183...\times10^{-78}\\ 4.202832669858257...*10^{-78}\end{array}$ 

The sum of the three results is:

 $(-3.15212450239369*10^{-78}) + (-2.10141633492912854*10^{-78}) + (4.202832669858257*10^{-78})$ 

# Input interpretation:

 $\begin{array}{l} -3.15212450239369 \times 10^{-78} \\ -2.10141633492912854 \times 10^{-78} \\ +4.202832669858257 \times 10^{-78} \end{array}$ 

#### **Result:**

 $-1.05070816746456154 \times 10^{-78}$ 

-1.05070816746456154 \* 10<sup>-78</sup>

The difference is:

(-3.15212450239369\*10^-78) - (-2.10141633492912854\*10^-78) - (4.202832669858257\*10^-78)

# Input interpretation:

 $\begin{array}{r} -3.15212450239369 \times 10^{-78} \\ -2.10141633492912854 \times 10^{-78} \\ -4.202832669858257 \times 10^{-78} \end{array}$ 

#### **Result:**

-5.25354083732281846 × 10<sup>-78</sup> -5.2535408373 \* 10<sup>-78</sup>

We have also:

$$\rho + p_r = \frac{2r_0^2}{r^6 V_0 \kappa^2} \left(10 - 11\frac{r_0^2}{r^2}\right),\tag{45}$$

$$\rho + p_t = \frac{4r_0^2}{r^6 V_0 \kappa^2} \left( -1 + \frac{r_0^2}{r^2} \right). \tag{46}$$

From the (45), we obtain:

2\*(1.90693^2) / ((((1.94973e+13)^6\*(-42)\*0.006))) \* (((10-11\*(1.90693^2)/  $((1.94973e+13)^2))))$ 

# Input interpretation:

 $2 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^6 \times (-42) \times 0.006} \left(10 - 11 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^2}\right)$ 

# **Result:**

-5.253540837322821353767036212975325323422722929362114... × 10<sup>-78</sup> -5.25354083732... \* 10<sup>-78</sup>

From the (46), we obtain:

4\*(1.90693^2) / ((((1.94973e+13)^6\*(-42)\*0.006))) \* (((-1+(1.90693^2)/ ((1.94973e+13)^2))))

Input interpretation:  $4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^6 \times (-42) \times 0.006} \left(-1 + \frac{1.90693^2}{(1.94973 \times 10^{13})^2}\right)$ 

# **Result:**

 $1.0507081674645642707534072436001497654085283318249645\ldots \times 10^{-78}$ 

 $1.05070816746456427...*10^{-78}$ 

from which:

(((4\*(1.90693^2) / ((((1.94973e+13)^6\*(-42)\*0.006))) \* (((-1+(1.90693^2)/ ((1.94973e+13)^2))))))^1/373

# **Input interpretation:**

$$\sqrt[373]{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^6 \times (-42) \times 0.006} \left(-1 + \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^2}\right)}$$

# **Result:**

0.6179343...

0.6179343... result that is a very good approximation to the value of the golden ratio conjugate 0,618033988749...

and:

 $\frac{1}{((((((4*(1.90693^{2}) / ((((1.94973e+13)^{6}*(-42)*0.006))) * (((-1+(1.90693^{2})/((1.94973e+13)^{2}))))))^{1/373})))}{((1.94973e+13)^{2}))))))^{1/373})))$ 

# **Input interpretation:**

$$373 \sqrt{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^6 \times (-42) \times 0.006} \left(-1 + \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^2}\right)}$$

# **Result:**

1.618295...

1.618295... result that is a very good approximation to the value of the golden ratio 1,618033988749...

From the ratio from (45) and (46), we have also:

 $\begin{array}{l} -[2*(1.90693^{2}) / \left(\left(\left((1.94973e^{+13})^{6}*(-42)*0.006\right)\right)\right)* \left(\left((10-11*(1.90693^{2}) / ((1.94973e^{+13})^{2}))\right)\right] \\ / \left[4*(1.90693^{2}) / \left(\left(\left((1.94973e^{+13})^{6}*(-42)*0.006\right)\right)\right)* \left(\left((-1.94973e^{+13})^{2}+13)^{2}\right)\right)\right)\right] \\ \end{array}$ 

# Input interpretation:

 $-\frac{2 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^6 \times (-42) \times 0.006} \left(10 - 11 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^2}\right)}{4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^6 \times (-42) \times 0.006} \left(-1 + \frac{1.90693^2}{(1.94973 \times 10^{13})^2}\right)}$ 

# **Result:**

4.99999999999999999999999999995217108175958474226426734009330...

**4.999999999**....≈ 5

from which:

```
 \left[ -\left[2*(1.90693^{2}) / \left(\left(\left(1.94973e+13\right)^{6}*(-42)*0.006\right)\right)\right) * \left(\left((10-11*(1.90693^{2}) / ((1.94973e+13)^{2}))\right)\right) \right] / \left[4*(1.90693^{2}) / \left(\left(\left(1.94973e+13\right)^{6}*(-42)*0.006\right)\right)\right) * \left(\left((-1+(1.90693^{2}) / ((1.94973e+13)^{2})))\right)\right] \right]^{3}
```

#### **Input interpretation:**

$$\left(-\frac{2 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^6 \times (-42) \times 0.006} \left(10 - 11 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^2}\right)}{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^6 \times (-42) \times 0.006} \left(-1 + \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^2}\right)}\right)^3$$

#### **Result:**

124.99999999999999999999999996412831131968855669820050510429...

124.99999999...≈ 125

#### and:

 $\begin{array}{l} [1/2((([-[2*(1.90693^{2})/((((1.9497e+13)^{6}*(-42)*0.006))))(((10-11*(1.90693^{2})/(((1.9497e+13)^{2}))))] / [4*(1.90693^{2})/((((1.9497e+13)^{6}*(-42)*0.006)))(((-1+(1.90693^{2})/(((1.9497e+13)^{2}))))]^{3}+3)))]^{2} \end{array}$ 

#### Input interpretation:

$$\left(\frac{1}{2} \left( \left(-\frac{2 \times \frac{1.90693^2}{\left(1.9497 \times 10^{13}\right)^6 \times (-42) \times 0.006} \left(10 - 11 \times \frac{1.90693^2}{\left(1.9497 \times 10^{13}\right)^2}\right)}{4 \times \frac{1.90693^2}{\left(1.9497 \times 10^{13}\right)^6 \times (-42) \times 0.006} \left(-1 + \frac{1.90693^2}{\left(1.9497 \times 10^{13}\right)^2}\right)}\right)^3 + 3 \right) \right)^2$$

#### **Result:**

4095.99999999999999999999999977041412734141170045035473194309...

4095.99999999....≈ 4096

 $\begin{array}{l} (((([1/2((([-[2(1.9069^2)/((((1.9497e+13)^6 (-42)0.006))) (((10-11(1.9069^2)/((1.9497e+13)^2))))] / [4(1.9069^2)/((((1.9497e+13)^6 (-42)0.006))) (((-1+(1.9069^2)/((1.9497e+13)^2))))] / [3+3)))]^2))))^{1/2} \end{array}$ 

# Input interpretation:

$$\sqrt{\left(\frac{1}{2}\left(\left(-\frac{2\times\frac{1.9069^2}{\left(1.9497\times10^{13}\right)^6\times\left(-42\right)\times0.006}\left(10-11\times\frac{1.9069^2}{\left(1.9497\times10^{13}\right)^2}\right)\right)^3+3\right)\right)^2+3}\right)^2$$

#### **Result:**

63.999999999999999999999999982064168048215986420689922093301...

**63.9999999**....≈ 64

# Now, we have:

the line element at the surface  $\Sigma$  and outside it is

$$ds^{2} = -\left(\frac{1 - \frac{2M}{r} - \frac{V_{0}(\varphi_{e} - \psi_{e})r^{2}}{6}}{1 - \frac{2M}{r_{\Sigma}} - \frac{V_{0}(\varphi_{e} - \psi_{e})r_{\Sigma}^{2}}{6}}\right)e^{\zeta_{0}}dt^{2} + (66) + \left(1 - \frac{2M}{r} - \frac{V_{0}(\varphi_{e} - \psi_{e})r^{2}}{6}\right)^{-1}dr^{2} + r^{2}d\Omega^{2},$$
  

$$r \ge r_{\Sigma}, \qquad (67)$$

and

$$\begin{split} [K] &= \frac{1}{r_{\Sigma}} \left[ \frac{r_0 \zeta_0}{2r_{\Sigma}} \sqrt{1 - \left(\frac{r_0}{r_{\Sigma}}\right)^2} - \sqrt{1 - \left(\frac{r_0}{r_{\Sigma}}\right)^4} \right. \\ &- \sqrt{1 - \left(\frac{r_0}{r_{\Sigma}}\right)^5} + \frac{2 - \frac{3M}{r_{\Sigma}} + \frac{r_0^2}{2r_{\Sigma}^2}}{\sqrt{1 - \frac{2M}{r_{\Sigma}} + \frac{r_0^2}{6r_{\Sigma}^2}}} \right] = 0. \end{split}$$
(74)

of the free parameters are  $\zeta_0 = -10.96$ , M = 1, the throat is at  $r_0 = 2\sqrt{10/11} = 1.907$ ,  $\psi_0 = 1$ ,  $\psi_1 = 0$ ,  $V_0 = -42$ , and the matching surface is at  $r_{\Sigma} = 2$ . The metric fields  $\zeta(r)$  and b(r) are asymptotically AdS, and a thin shell of matter is perceptibly present at the matching surface  $r_{\Sigma} = 2$  (more properly at  $r_{\Sigma} = 2M$  in our solution, and here we put M = 1), thus outside

From the above data, we obtain from (74):

$$\begin{array}{l} 1/2 \left( \left( \left( \left( \left( \left( \left( 1.907^* - 10.96 \right) / 4^* \left( 1 - \left( 1.907 / 2 \right)^2 \right)^2 \right)^2 1 / 2 - \left( 1 - \left( 1.907 / 2 \right)^4 \right)^2 1 / 2 - \left( 1 - \left( 1.907 / 2 \right)^2 \right)^2 \right)^2 \right) \\ (1.907 / 2)^5 \right)^2 1/2 + \left( 2 - 3 / 2 + \left( 1.907 ^2 \right) / \left( 2^* 2^2 2 \right) \right) / \left( 1 - 2 \left( 13.12806 e^{+13} \right) / 2 + \left( 1.907 ^2 \right) / \left( 6^* 2^2 2 \right) \right)^2 1 / 2 \right) \right) \right) \right) \\ \end{array}$$

Input:

$$\frac{1}{2} \left[ \left( \frac{1}{4} \left( 1.907 \times (-10.96) \right) \right) \sqrt{1 - \left( \frac{1.907}{2} \right)^2} - \sqrt{1 - \left( \frac{1.907}{2} \right)^5} - \sqrt{1 - \left( \frac{1.907}{2} \right)^5} + \frac{2 - \frac{3}{2} + \frac{1.907^2}{2 \times 2^2}}{\sqrt{1 - \frac{2}{2} + \frac{1.907^2}{6 \times 2^2}}} \right]$$

#### **Result:**

0.000354984245465581426559927406802318322121150629066455452... 0.000354984245...

Or:

for  $\zeta_0 = -10.96$ ,  $r_0 = 2\sqrt{10/11} = 1.90693$ 

M = 13.12806e+39, r = 1.94973e+13, we obtain:

 $\frac{1}{1.94973e+13[(((((1.907*-10.96)/(2(1.94973e+13))*(-1))))) + ((2-(3*13.12806e+39)/(1.94973e+13))+(1.907^{2})/(2*(1.94973e+13)^{2}))/(1-2(13.12806e+39)/(1.94973e+13)+(1.907^{2})/(6*(1.94973e+13)^{2}))^{1/2}]$ 

# Input interpretation:

$$\frac{1}{1.94973\times10^{13}} \left( \frac{1.907\times(-10.96)}{2\times1.94973\times10^{13}}\times(-1) + \frac{\left(2-\frac{3\times13.12806\times10^{39}}{1.94973\times10^{13}}\right) + \frac{1.907^2}{2\left(1.94973\times10^{13}\right)^2}}{\sqrt{1-2\times\frac{13.12806\times10^{39}}{1.94973\times10^{13}} + \frac{1.907^2}{6\left(1.94973\times10^{13}\right)^2}}}\right)$$

**Result:** 2.74905... × 10<sup>-26</sup> + 2.82322... *i* 

#### **Polar coordinates:**

r = 2.82322 (radius),  $\theta = 90^{\circ}$  (angle) 2.82322

from which:

# Input interpretation:

 $-\frac{47}{34+5}i + \frac{1}{1.9497 \times 10^{13}} \left( -\frac{1.907 \times (-10.96)}{2 \times 1.9497 \times 10^{13}} + \frac{\left(2 - \frac{3 \times 13.128 \times 10^{39}}{1.9497 \times 10^{13}}\right) + \frac{1.907^2}{2\left(1.9497 \times 10^{13}\right)^2}}{\sqrt{1 - 2 \times \frac{13.128 \times 10^{39}}{1.9497 \times 10^{13}} + \frac{1.907^2}{6\left(1.9497 \times 10^{13}\right)^2}}}\right)$ 

i is the imaginary unit

#### **Result:**

2.74913...×10<sup>-26</sup> + 1.61815...*i* 

#### **Polar coordinates:**

r = 1.61815 (radius),  $\theta = 90^{\circ}$  (angle)

1.61815 result that is a very good approximation to the value of the golden ratio 1,618033988749...

Note that:

# golden ratio\*i+(47/(34+5))i

Input:  $\phi i + \frac{47}{34+5}i$ 

\$\overline is the golden ratio
\$\overline is the imaginary unit

**Result:** 

 $i\phi + \frac{47i}{39}$ 

#### **Decimal approximation:**

2.823162193878099976409715039493843245925437384933967990340... i

# **Polar coordinates:**

 $r \approx 2.82316$  (radius),  $\theta = 90^{\circ}$  (angle) 2.82316

# Alternate forms:

 $\frac{1}{78} i \left( 133 + 39 \sqrt{5} \right)$  $i \left( \phi + \frac{47}{39} \right)$  $\frac{1}{39} i (39 \phi + 47)$ 

# Alternative representations:

 $\phi i + \frac{i47}{34+5} = \frac{47i}{39} + 2i\sin(54^\circ)$  $\phi i + \frac{i47}{34+5} = -2i\cos(216^\circ) + \frac{47i}{39}$  $\phi i + \frac{i47}{34+5} = \frac{47i}{39} - 2i\sin(666^\circ)$ 

We have the following Ramanujan expression for obtain the golden ratio:

 $(((((1/(((1/32(-1+sqrt(5))^{5}+5*(e^{(-sqrt(5)*Pi)})^{5})))-(9.99290225070718723070536304129457122742436976265255\times10^{-7428})-(1.01567312386781438874777576295646917898823529098784\times10^{-7427})))))^{1/5}$ 

Input interpretation:  $\begin{pmatrix} 1 / \left( \left( \frac{1}{32} \left( -1 + \sqrt{5} \right)^5 + 5 e^{\left( -\sqrt{5} \pi \right)^5} \right) - \\ \frac{9.99290225070718723070536304129457122742436976265255}{10^{7428}} - \\ \frac{101567312386781438874777576295646917898823529098784}{10^{7427}} \right) \right)^{-} (1/5)$ 

# **Result:**

 $1.618033988749894848204586834365638117720309179805762862135\ldots$ 

 $\phi \approx 1.618033988749894848204586834365638117720309179805762862135$ 

 $\begin{array}{l} \Phi + 1 \approx 1.618033988749894848204586834365638117720309179805762862135\\ \frac{1}{\Phi} \approx 1.618033988749894848204586834365638117720309179805762862135 \end{array}$ 

Or:

((((1/(((1/32(-1+sqrt(5))^5+5\*(e^((sqrt(5)\*Pi))^5)))+(1.6382898797095665677239458827012056245798314722584 × 10^-7429)))^1/5

# Input interpretation:

 $\sqrt[5]{\frac{1}{\left(\frac{1}{32}\left(-1+\sqrt{5}\right)^{5}+5\,e^{\left(-\sqrt{5}\,\pi\right)^{5}}\right)+\frac{1.6382898797095665677239458827012056245798314722584}{10^{7429}}}}$ 

# **Result:**

 1.618033988749894848204586834365638117720309179805762862135...

 1.618033988749894848204586834365638117720309179805762862135

# **Possible closed forms:**

```
\begin{split} \phi &\approx 1.61803398874989484820458683436563811772030917980576286213544862 \\ \Phi + 1 &\approx \\ 1.61803398874989484820458683436563811772030917980576286213544862 \\ \frac{1}{\Phi} &\approx 1.61803398874989484820458683436563811772030917980576286213544862 \end{split}
```

 $\phi$  is the golden ratio  $\Phi$  is the golden ratio conjugate

We have the following mathematical connection:

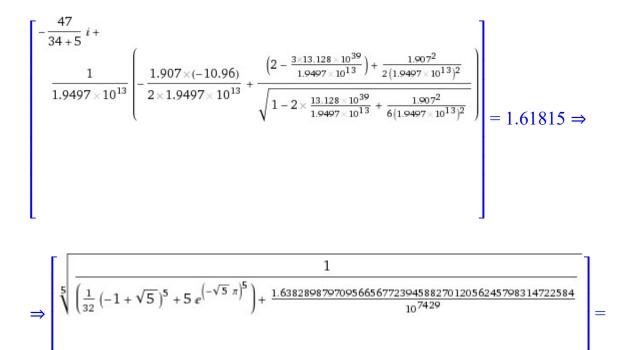
$$-\frac{47}{34+5}i + \frac{1}{1.9497 \times 10^{13}} \left( -\frac{1.907 \times (-10.96)}{2 \times 1.9497 \times 10^{13}} + \frac{\left(2 - \frac{3 \times 13.128 \times 10^{39}}{1.9497 \times 10^{13}}\right) + \frac{1.907^2}{2\left(1.9497 \times 10^{13}\right)^2}}{\sqrt{1 - 2 \times \frac{13.128 \times 10^{39}}{1.9497 \times 10^{13}} + \frac{1.907^2}{6\left(1.9497 \times 10^{13}\right)^2}}}\right)$$

1.61815

$$\sqrt{\frac{1}{\left(\frac{1}{32}\left(-1+\sqrt{5}\right)^{5}+5\ e^{\left(-\sqrt{5}\ \pi\right)^{5}}\right)+\frac{1.6382898797095665677239458827012056245798314722584}{10^{7429}}}}$$

#### 1.618033988749894848204586834365638117720309179805762862135

Thence:



#### = 1.618033988749894848204

 $1.61815 \approx 1.618033988 =$  golden ratio

Now, we have that:

$$\begin{bmatrix} K_0^0 \end{bmatrix} = \frac{r_0 \zeta_0}{2r_{\Sigma}^2} \sqrt{1 - \frac{r_0^2}{r_{\Sigma}^2}} + \frac{\frac{r_0^2}{r_{\Sigma}} - 6M}{6r_{\Sigma}^2 \sqrt{1 - \frac{2M}{r_{\Sigma}} + \frac{r_0^2}{6r_{\Sigma}^2}}}.$$
 (71)

for  $\zeta_0 = -10.96$ ,  $r_0 = 2\sqrt{10/11} = 1.90693$ 

M = 13.12806e+39,  $r = r_{\Sigma} = 1.94973e+13$ , we obtain:

 $\begin{array}{l} (1.90693^{*}(-10.96))/(2(1.94973e+13)^{2})^{*}(((1-(1.90693^{2})/((1.94973e+13)^{2})))^{1/2} + ((1.90693^{2})/(1.94973e+13))^{-}(6^{*}(13.12806e+39))^{*}1/[\\ 6^{*}(1.94973e+13)^{2}^{*}((((1-(2^{*}(1.312806e+39))/((1.94973e+13))))^{1/2}] \\ \end{array}$ 

 $(1.90693^{(-10.96)})/(2(1.94973e^{+13})^{2})^{((1-(1.90693^{2})/((1.94973e^{+13})^{2})))^{1/2} + ((1.90693^{2})/(1.94973e^{+13}))^{-(6^{(13.12806e^{+39}))})^{-(6^{(13.12806e^{+39})})^{-(6^{(13.12806e^{+39}))})^{-(6^{(13.12806e^{+39}))})^{-(6^{(13.12806e^{+39}))})^{-(6^{(13.1280e^{+39})})^{-(6^{(13.1280e^{+39}))})^{-(6^{(13.1280e^{+39})})^{-(6^{(13.1280e$ 

#### **Input interpretation:**

 $\frac{1.90693 \times (-10.96)}{2 \left(1.94973 \times 10^{13}\right)^2} \sqrt{1 - \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^2}} + \frac{1.90693^2}{1.94973 \times 10^{13}} - 6 \times 13.12806 \times 10^{39}$ 

#### **Result:**

-7.876835999...\*10<sup>40</sup>

 $(-7.87683599 \times 10^{40})*1/[6*(1.94973e+13)^{2}(((1-(2*(13.12806e+39))/((1.94973e+13))+(1.90693^{2})/(6*(1.94973e+13)^{2})))^{1/2}]$ 

#### Input interpretation:

 $-7.87683599 \times 10^{40} \times \frac{1}{6 \left(1.94973 \times 10^{13}\right)^2 \sqrt{1 - \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{1.90693^2}{6 \left(1.94973 \times 10^{13}\right)^2}}$ 

#### **Result:**

0.941074... i

#### **Polar coordinates:**

r = 0.941074 (radius),  $\theta = 90^{\circ}$  (angle) 0.941074

from which:

 $(((((-7.87683599 \times 10^{4}0)/[6*(1.94973e+13)^{2}*(((1-(2*(13.12806e+39))/((1.94973e+13))+(1.90693^{2})/(6*(1.94973e+13)^{2}))))^{1/2}]))))^{1/64}$ 

# Input interpretation:

$$\sqrt[64]{ - \frac{7.87683599 \times 10^{40}}{6 \left(1.94973 \times 10^{13}\right)^2 \sqrt{1 - \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{1.90693^2}{6 \left(1.94973 \times 10^{13}\right)^2} } } } }$$

#### **Result:**

0.9987506... + 0.02451795... i

#### **Polar coordinates:**

r = 0.999051 (radius),  $\theta = 1.40625^{\circ}$  (angle)

0.999051 result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and:

2log base 0.9990515[((((i\*-(-7.87683599 × 10^40)/[ 6\*(1.94973e+13)^2\*(((1-(2\*(13.12806e+39))/((1.94973e+13))+(1.90693^2)/(6\*(1.94973e+13)^2))))^1/2])))]-Pi+1/golden ratio

# Input interpretation:

$$2 \log_{0.9990515} \left( i \left( -\frac{-7.87683599 \times 10^{40}}{6 \left( 1.94973 \times 10^{13} \right)^2 \sqrt{1 - \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{1.90693^2}{6 \left( 1.94973 \times 10^{13} \right)^2}} \right) \right) - \pi + \frac{1}{\phi} \right)$$

 $\log_{b}(x)$  is the base- b logarithm

i is the imaginary unit

 $\phi$  is the golden ratio

# **Result:**

125.479...

# 125.479... result very near to the Higgs boson mass 125.18 GeV

2log base  $0.9990515[((((i*-(-7.87683599 \times 10^{40})/[6*(1.94973e+13)^2*(((1-(2*(13.12806e+39))/((1.94973e+13))+(1.90693^2)/(6*(1.94973e+13)^2))))^1/2]))))] +8+golden ratio$ 

# Input interpretation:

$$2 \log_{0.9990515} \left[ i \left[ - \frac{-7.87683599 \times 10^{40}}{6 \left( 1.94973 \times 10^{13} \right)^2 \sqrt{1 - \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{1.90693^2}{6 \left( 1.94973 \times 10^{13} \right)^2}} \right] \right] + 8 + \phi$$

 $\log_b(x)$  is the base- b logarithm

11

i is the imaginary unit

 $\phi$  is the golden ratio

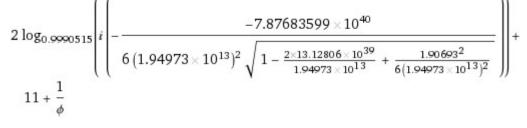
#### **Result:**

137.621...

137.621... result practically equal to the golden angle value 137.5

2log base  $0.9990515[((((i*-(-7.87683599 \times 10^{40})/[6*(1.94973e+13)^2*(((1-(2*(13.12806e+39))/((1.94973e+13))+(1.90693^2)/(6*(1.94973e+13)^2))))^{1/2}]))))] +11+1/golden ratio$ 

#### **Input interpretation:**



 $\log_b(x)$  is the base– b logarithm i is the imaginary unit  $\phi$  is the golden ratio

#### **Result:**

139.621...

139.621... result practically equal to the rest mass of Pion meson 139.57 MeV

 $\begin{array}{l} 27*\log base \ 0.9990515[(((((i*-(-7.87683599 \times 10^{4}0)/[\ 6*(1.94973e+13)^{2}*(((1-(2*(13.12806e+39))/((1.94973e+13))+(1.90693^{2})/(6*(1.94973e+13)^{2}))))^{1/2}]))))] \\ +1 \end{array}$ 

#### **Input interpretation:**

$$27 \log_{0.9990515} \left[ i \left[ -\frac{-7.87683599 \times 10^{40}}{6 \left( 1.94973 \times 10^{13} \right)^2 \sqrt{1 - \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{1.90693^2}{6 \left( 1.94973 \times 10^{13} \right)^2}} \right] \right] + 1$$

 $\log_b(x)$  is the base- b logarithm i is the imaginary unit

11

#### **Result:**

1729.03... 1729.03...

This result is very near to the mass of candidate glueball  $f_0(1710)$  scalar meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number) With regard 27 (From Wikipedia):

"The fundamental group of the complex form, compact real form, or any algebraic version of  $E_6$  is the cyclic group  $\mathbb{Z}/3\mathbb{Z}$ , and its outer automorphism group is the cyclic group  $\mathbb{Z}/2\mathbb{Z}$ . Its fundamental representation is 27-dimensional (complex), and a basis is given by the 27 lines on a cubic surface. The dual representation, which is inequivalent, is also 27-dimensional. In particle physics,  $E_6$  plays a role in some grand unified theories".

and again:

(27 log(0.9990515, (i (-(-7.87683599×10^40)))/(6 (1.94973×10^13)^2 sqrt(1 - (2 13.12806×10^39)/(1.94973×10^13) + 1.90693^2/(6 (1.94973×10^13)^2)))) + 1)^(1/15)

#### **Input interpretation:**

$$\frac{i\left(-\left(-7.87683599\times10^{40}\right)\right)}{6\left(1.94973\times10^{13}\right)^2\sqrt{1-\frac{2\times13.12806\times10^{39}}{1.94973\times10^{13}}+\frac{1.90693^2}{6\left(1.94973\times10^{13}\right)^2}}\right)+1$$

 $\log_b(x)$  is the base- b logarithm

i is the imaginary unit

# **Result:**

1.643817346898998754390794286147616625111556020183173634676...

$$1.643817346898... \approx \zeta(2) = \frac{\pi^2}{6} = 1.644934...$$

(27 log(0.9990515, (i (-(-7.87683599×10^40)))/(6 (1.94973×10^13)^2 sqrt(1 - (2 13.12806×10^39)/(1.94973×10^13) + 1.90693^2/(6 (1.94973×10^13)^2)))) + 1)^(1/15) -(21+5)1/10^3

#### **Input interpretation:**

$$\frac{15}{\sqrt{27 \log_{0.9990515} \left( \frac{i \left( - \left( -7.87683599 \times 10^{40} \right) \right)}{6 \left( 1.94973 \times 10^{13} \right)^2 \sqrt{1 - \frac{2 \times 13.12806 \times 10^{39}}{1.94973 \times 10^{13}} + \frac{1.90693^2}{6 \left( 1.94973 \times 10^{13} \right)^2} \right)} + 1 - \frac{1}{10^3} + \frac{1}{10^3$$

 $\log_b(x)$  is the base- b logarithm i is the imaginary unit

#### **Result:**

1.617817346898998754390794286147616625111556020183173634676...

1.617817346898... result that is a very good approximation to the value of the golden ratio 1,618033988749...

Now, we have that:

Then,  $\sigma$  and p are given by

$$\sigma = \frac{4r_0^2}{\kappa^2 V_0 r_{\Sigma}^5} \left( 1 - \frac{1}{4} r_{\Sigma} \left[ K_0^0 \right] \right) \,, \tag{72}$$

$$p = -\frac{4r_0^2}{\kappa^2 V_0 r_{\Sigma}^5} \left( 1 + \frac{1}{8} r_{\Sigma} \left[ K_0^0 \right] \right) \,, \tag{73}$$

For K = 0.941074 V<sub>0</sub> = -42

 $\zeta_0 = -10.96, \quad r_0 = 2\sqrt{10/11} = 1.90693$ 

M = 13.12806e+39,  $r = r_{\Sigma} = 1.94973e+13$ , we obtain:

4\*(1.90693^2) / ((((1.94973e+13)^5\*(-42)\*0.006)))\*(((1-1/4\*((1.94973e+13)\*0.941074))))

Input interpretation:  $4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)$ 

#### **Result:**

 $9.3971214538910565083220941663988465977813055160575214...\times 10^{-53}$ 9.39712145389...\*10<sup>-53</sup>

-4\*(1.90693^2) / ((((1.94973e+13)^5\*(-42)\*0.006)))\*(((1+1/8\*((1.94973e+13)\*0.941074))))

# **Input interpretation:**

 $-4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)$ 

**Result:** 4.6985607269486011500140731105428473599776441949350642... × 10<sup>-53</sup> 4.69856072694...\*10<sup>-53</sup>

We note that the ratio between the two results is:

 $\begin{array}{l} \textbf{Input interpretation:} \\ - \frac{4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}{4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)} \right) \end{array}$ 

# **Result:**

1.999999999998691984191924378378871462016694888973494180351... $1.99999999... \approx 2$  result practically equal to the graviton spin

and:

 $\left[ \left( 4^{*}(1.90693^{2}) / \left( \left( \left( (1.94973e^{+}13)^{5}(-42)^{*}0.006 \right) \right) \right)^{*}(\left( (1-1/4^{*}((1.94973e^{+}13)^{*}0.941074) \right) \right) \right) / \left( -4^{*}(1.90693^{2}) / \left( \left( \left( (1.94973e^{+}13)^{5}(-42)^{*}0.006 \right) \right) \right)^{*}(\left( (1+1/8^{*}((1.94973e^{+}13)^{*}0.941074) \right) ) ) ) \right)^{7} + 11 - 2 + 1/2 \right)$ 

# **Input interpretation:**

$$\left(-\frac{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}\right)^7 + 11 - 2 + \frac{1}{2} \times 10^{13} \times 10^{13}$$

# **Result:**

137.499999994140089179832712421324198150515819376122576666... $137.499999... \approx 137.5$  result practically equal to the golden angle value 137.5

# **Input interpretation:**

 $\left(-\frac{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}\right)^7 + 11 + 0.618034$ 

# **Result:**

139.6180339994140089179832712421324198150515819376122576666...

139.618033999... result practically equal to the rest mass of Pion meson 139.57  $\,\mathrm{MeV}$ 

#### **Input interpretation:**

$$\left(-\frac{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}\right)^7 - \pi + 0.618034$$

# **Result:**

125.476...

125.476... result very near to the Higgs boson mass 125.18 GeV

 $\begin{array}{l} 27*1/2*[(4*(1.90693^{2}) / ((((1.94973e+13)^{5*}(-42)*0.006)))*(((1-1/4*((1.94973e+13)*0.941074))))) / (-4*(1.90693^{2}) / ((((1.94973e+13)^{5*}(-42)*0.006)))*(((1+1/8*((1.94973e+13)*0.941074)))))]^{7+1} \end{array}$ 

#### Input interpretation:

$$27 \times \frac{1}{2} \left( -\frac{4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}{4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)} \right)^7 + 1 \times 10^{13} \times 10$$

# **Result:** 1728.99999992089120392774161768787667503196356157765478500... 1728.99999... ≈ 1729

This result is very near to the mass of candidate glueball  $f_0(1710)$  scalar meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

and again:

$$\begin{aligned} &\ln(((27*1/2[(4(1.9069^2)/((((1.9497e+13)^5(-42)*0.006))))(((1-1/4)((1.9497e+13)0.941074)))))/(-4(1.9069^2)/((((1.9497e+13)^5(-42)*0.006))))(((1+1/8)((1.9497e+13)0.941074)))))]^{7+1})))^{1/3} - (0.322+0.013) \end{aligned}$$

#### **Input interpretation:**

$$\sqrt[3]{\log\left[27 \times \frac{1}{2} \left(-\frac{4 \times \frac{1.9069^2}{(1.9497 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.9497 \times 10^{13} \times 0.941074\right)\right)}{4 \times \frac{1.9069^2}{(1.9497 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.9497 \times 10^{13} \times 0.941074\right)\right)}\right)^7 + 1\right) - (0.322 + 0.013)}$$

log(x) is the natural logarithm

# **Result:**

1.61854...

1.61854... result that is a very good approximation to the value of the golden ratio 1,618033988749...

where 199 is a Lucas number and 0.08181636 is the value of the following sum of two Ramanujan mock theta functions: 0.9243408 (i) - 1.00615716 (ii) = -0.08181636

Mock  $\vartheta$ -functions (of 7th order)

(i) 
$$1 + \frac{q}{1-q^2} + \frac{q^4}{(1-q^3)(1-q^4)} + \frac{q^9}{(1-q^4)(1-q^5)(1-q^6)} + \dots$$

(ii) 
$$\frac{q}{1-q} + \frac{q}{(1-q^2)(1-q^3)} + \frac{q}{(1-q^3)(1-q^4)(1-q^5)} + \dots$$

(iii) 
$$\frac{1}{1-q} + \frac{q^2}{(1-q^2)(1-q^3)} + \frac{q^5}{(1-q^3)(1-q^4)(1-q^5)} + \dots$$

## Input interpretation:

$$\frac{\overline{10^{27}}}{\left[\sqrt[3]{\log\left[27 \times \frac{1}{2}\left(-\frac{4 \times \frac{1.9069^2}{(1.9497 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.9497 \times 10^{13} \times 0.941\right)\right)}{4 \times \frac{1.9069^2}{(1.9497 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.9497 \times 10^{13} \times 0.941\right)\right)}\right)^7 + 1\right]} - (0.199 + 0.08181636)\right]}$$

log(x) is the natural logarithm

#### **Result:**

 $1.67272... \times 10^{-27}$  $1.67272... \times 10^{-27}$  result practically equal to the proton mass

and performing the following integrals, we obtain:

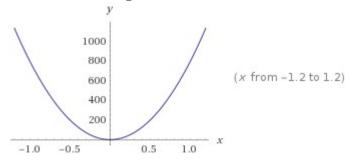
int [12[(4(1.90693^2) / ((((1.94973e+13)^5 (-42)0.006)))\*(((1-1/4((1.94973e+13)0.941074))))) / (-4(1.90693^2) / (((((1.94973e+13)^5 (-42)0.006)))\*(((1+1/8((1.94973e+13)0.941074)))))]^7+29]x

# **Indefinite integral:**

$$\int \left( 12 \left( \frac{4 \times 1.90693^2 \left( 1 - \frac{1}{4} \ 1.94973 \times 10^{13} \ 0.941074 \right)}{\left( (1.94973 \times 10^{13})^5 \ (-42)0.006 \right) \left( -4 \times 1.90693^2 \left( 1 + \frac{1}{8} \ 1.94973 \times 10^{13} \ 0.941074 \right) \right)}{(1.94973 \times 10^{13})^5 \ (-42)0.006} \right)^7 + 29 \right) x \, dx = 782.5 \ x^2 + \text{constant}$$

782.5 (for x = 1) result practically equal to the rest mass of Omega meson 782.65

# Plot of the integral:



# Alternate form assuming x is real:

**782.5** x<sup>2</sup> + 0 + constant

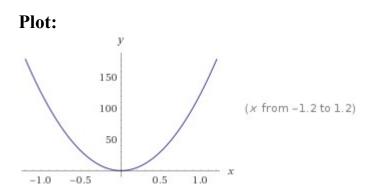
1/(2Pi) int [12[(4(1.90693^2) / ((((1.94973e+13)^5 (-42)0.006)))\*(((1-1/4((1.94973e+13)0.941074))))) / (-4(1.90693^2) / (((((1.94973e+13)^5 (-42)0.006)))\*(((1+1/8((1.94973e+13)0.941074)))))]^7+29]x

# Input interpretation:

$$\frac{1}{2\pi} \int \left( 12 \left( -\left( \left( 4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \right)^{1/2} \left( 1 - \frac{1}{4} (1.94973 \times 10^{13} \times 0.941074) \right) \right) \right) \right) \right) \\ \left( 4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \right) \\ \left( 1 + \frac{1}{8} (1.94973 \times 10^{13} \times 0.941074) \right) \right) \right) \right)^7 + 29 \right) x \, dx$$

#### **Result:**

124.539  $x^2$ 124.539 (for x = 1) result very near to the Higgs boson mass 125.18 GeV



Alternate form assuming x is real:  $124.539 x^2 + 0$ 

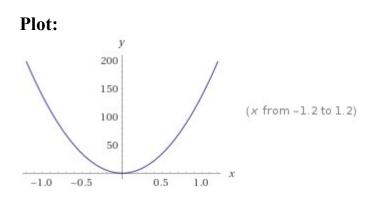
 $\frac{1}{(Pi+256/10^{2}) int [12[(4(1.90693^{2})/((((1.94973e+13)^{5}(-42)0.006)))(((1-1/4)((1.94973e+13)0.941074)))))/(-4(1.90693^{2})/((((1.94973e+13)^{5}(-42)0.006)))(((1+1/8)((1.94973e+13)0.941074)))))^{7+29}]x}$ 

#### **Input interpretation:**

$$\begin{aligned} \frac{1}{\pi + \frac{256}{10^2}} & \int \left( 12 \left( -\left( \left( 4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \right)^{1/3} + \left( 1.94973 \times 10^{13} \times 0.941074 \right) \right) \right) \right) \right) \\ & \left( 1 - \frac{1}{4} \left( 1.94973 \times 10^{13} \times 0.941074 \right) \right) \right) \right) \\ & \left( 4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \right) \\ & \left( 1 + \frac{1}{8} \left( 1.94973 \times 10^{13} \times 0.941074 \right) \right) \right) \right) \\ \end{pmatrix}^7 + 29 \right) x \, dx \end{aligned}$$

# **Result:**

137.242  $x^2$ 137.242 (for x = 1) result practically equal to the golden angle value 137.5



# Alternate form assuming x is real:

 $137.242 x^2 + 0$ 

We obtain also:

 $\begin{array}{l} [27*1/2*[(4*(1.90693^{2}) / ((((1.94973e+13)^{5*}(-42)*0.006)))*(((1-1/4*((1.94973e+13)*0.941074))))) / (-4*(1.90693^{2}) / (((((1.94973e+13)^{5*}(-42)*0.006)))*(((1+1/8*((1.94973e+13)*0.941074)))))]^{7+1}^{1/15} \end{array}$ 

Input interpretation:

$$15 \sqrt{ 27 \times \frac{1}{2} \left( - \frac{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}{4 \times \frac{1.90693^2}{\left(1.94973 \times 10^{13}\right)^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)} \right)^7 + 1}$$

# **Result:**

 $1.643815228748226722275820309871744734726052239752646039423\ldots$ 

$$1.643815228748... \approx \zeta(2) = \frac{\pi^2}{6} = 1.644934...$$

and:

 $\begin{array}{l} [27*1/2[(4(1.90693^{2}) / ((((1.94973e+13)^{5} (-42)0.006)))*(((1-1/4)((1.94973e+13)0.941074))))) / (-4(1.90693^{2}) / ((((1.94973e+13)^{5} (-42)0.006)))*(((1+1/8)((1.94973e+13)0.941074)))))]^{7+1}^{1/15-0.026} \end{array}$ 

# Input interpretation:

$$15 \sqrt{ 27 \times \frac{1}{2} \left( -\frac{4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 - \frac{1}{4} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)}{4 \times \frac{1.90693^2}{(1.94973 \times 10^{13})^5 \times (-42) \times 0.006} \left(1 + \frac{1}{8} \left(1.94973 \times 10^{13} \times 0.941074\right)\right)} \right)^7 + 1 - 0.026} \right)}$$

# **Result:**

 $1.617815228748226722275820309871744734726052239752646039423\ldots$ 

1.617815228748... result that is a very good approximation to the value of the golden ratio 1,618033988749...

Now, we have that:

$$ds^{2} = -\left(1 - \frac{2GM}{c^{2}r} - \frac{\Lambda_{\text{ext}}}{3}r^{2}\right)c^{2}dt^{2} + \frac{dr^{2}}{\left(1 - \frac{2GM}{c^{2}r} - \frac{\Lambda_{\text{ext}}}{3}r^{2}\right)} + r^{2}\left(d\theta^{2} + \sin^{2}\theta \,d\phi^{2}\right).$$
(40)

#### (ii) The Schwarzschild-de Sitter spacetime, $\Lambda_{ext} > 0$

Equation (40) with  $\Lambda_{\text{ext}} > 0$  represents a black hole in asymptotically de Sitter space. If  $0 < 9\Lambda_{\text{ext}}(GMc^{-2})^2 < 1$ , the factor  $f(r) = (1 - \frac{2GM}{c^2r} - \frac{\Lambda_{\text{ext}}}{3}r^2)$ is zero at two positive values of r, corresponding to two real positive roots. Defining

$$A = \left(\frac{3c^4}{8\Lambda_{\text{ext}}G^2M^2}\right)^{1/3} \sqrt[3]{-1 + \sqrt{1 - \frac{c^4}{9\Lambda_{\text{ext}}G^2M^2}}},$$
 (42)

$$B = \left(\frac{3c^4}{8\Lambda_{\text{ext}}G^2M^2}\right)^{1/3} \sqrt[3]{-1 - \sqrt{1 - \frac{c^4}{9\Lambda_{\text{ext}}G^2M^2}}}, \quad (43)$$

the solutions are given by

$$r_b = \frac{2GM}{c^2} \left( -\frac{A+B}{2} - \frac{A-B}{2} \sqrt{-3} \right), \qquad (44)$$

$$r_c = \frac{2GM}{c^2}(A+B).$$
 (45)

When  $\Lambda_{\text{ext}}(GM/c^2)^2 \ll 1$  (see appendix A for details), one gets

$$r_b = \frac{2GM}{c^2} \left[ 1 + \frac{4}{3} \Lambda_{\text{ext}} \left( \frac{GM}{c^2} \right)^2 \right], \qquad (46)$$

$$r_c = \sqrt{\frac{3}{\Lambda_{\text{ext}}}} \left( 1 - \frac{GM}{c^2} \sqrt{\frac{\Lambda_{\text{ext}}}{3}} \right) . \tag{47}$$

From

$$A = \left(\frac{3c^4}{8\Lambda_{\rm ext}G^2M^2}\right)^{1/3} \sqrt[3]{-1 + \sqrt{1 - \frac{c^4}{9\Lambda_{\rm ext}G^2M^2}}},$$

for c = 299792458,  $\Lambda_{ext} = 1.1056e-52$ , G = 6.6743e-11 and M = 13.12806e+39, we obtain:

#### Input interpretation:

 $\sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \\ \sqrt[3]{-1 + \sqrt{1 - \frac{299\,792\,458^4}{(9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} }$ 

#### **Result:**

 $4.22412... \times 10^{12} + 2.43880... \times 10^{12} i$ 

#### **Polar coordinates:**

 $r = 4.8776 \times 10^{12}$  (radius),  $\theta = 30.^{\circ}$  (angle) 4.8776\*10<sup>12</sup>

From

$$B = \left(\frac{3c^4}{8\Lambda_{\rm ext}G^2M^2}\right)^{1/3} \sqrt[3]{-1 - \sqrt{1 - \frac{c^4}{9\Lambda_{\rm ext}G^2M^2}}},$$

we obtain:

#### Input interpretation:

$$\sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \\ \sqrt[3]{-1 - \sqrt{1 - \frac{299\,792\,458^4}{(9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}}}$$

**Result:** 

 $4.22412... \times 10^{12} - 2.43880... \times 10^{12} i$ 

# **Polar coordinates:**

 $r = 4.8776 \times 10^{12}$  (radius),  $\theta = -30.^{\circ}$  (angle) 4.8776\*10<sup>12</sup> Practically the same result as above.

Thence, multiplying by 2, we obtain A + B:

# Input interpretation:

$$2 \sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \sqrt[3]{-1 + \sqrt{1 - \frac{299\,792\,458^4}{(9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}}}$$

# **Result:**

 $8.44825... \times 10^{12} + 4.87760... \times 10^{12} i$ 

# **Polar coordinates:**

 $r = 9.7552 \times 10^{12}$  (radius),  $\theta = 30.^{\circ}$  (angle) 9.7552\*10<sup>12</sup>

From which:

```
[2[((((((3*299792458^4)/(((8*1.1056e-52)*(6.6743e-
11)^2(13.12806e+39)^2))))))^1/3*((((((-1+sqrt((((1-((((299792458^4)/(((9*1.1056e-
52)*(6.6743e-11)^2(13.12806e+39)^2)))))))))))))))))1/3]]^1/62
```

# Input interpretation:

$$\left( 2 \left[ \sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}} \right] \right) \right)^{-1} + \sqrt{1 - \frac{299\,792\,458^4}{(9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}} \right) \right)^{-1}$$

$$(1/62)$$

#### **Result:**

1.619900... + 0.01368061... i

# **Polar coordinates:**

r = 1.61996 (radius),  $\theta = 0.483871^{\circ}$  (angle)

1.61996 result that is a very good approximation to the value of the golden ratio 1,618033988749...

# or:

# Input interpretation:

$$\left( 2 \left[ \sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \right] \right) \\ \left[ \sqrt[3]{\frac{1}{9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}}{(9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \right] \right) \\ \left( \frac{1}{63} + \frac{11}{10^3} \right)$$

# **Result:**

1.618546... + 0.01336077... i

# **Polar coordinates:**

r = 1.6186 (radius),  $\theta = 0.472954^{\circ}$  (angle)

1.6186 result that is a very good approximation to the value of the golden ratio 1,618033988749...

We have also:

 $[2[((3*(3e+8)^4)/(((8*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2)))^{1/3*}[-1+sqrt((1-(((((3e+8)^4)/(((9*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))]^{1/3}]^{0.166666-8-0.47}$ 

where  $0.47 = 47 / 10^2$  (47 is a Lucas number) and 0.166666... is equal to 1/3

# Input interpretation:

 $\left( 2 \left( \sqrt[3]{\frac{3 (3 \times 10^8)^4}{(8 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}}_{8 - 0.47} \sqrt[3]{-1 + \sqrt{1 - \frac{(3 \times 10^8)^4}{(9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}}} \right) \right)^{0.100000} - \frac{100000}{(9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}} \right)^{0.100000} - \frac{100000}{(9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}}{(13.12806 \times 10^{39})^2} \left( \frac{100000}{(10 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}}{(13.12806 \times 10^{39})^2} \right)^{0.100000} - \frac{100000}{(10 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}}{(13.12806 \times 10^{39})^2} \left( \frac{100000}{(10 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}}{(13.12806 \times 10^{39})^2} \right)^{0.100000} - \frac{100000}{(10 \times 10^{-52}) (10 \times 10^{-52}) (1$ 

# **Result:**

137.179... + 12.7426... i

# **Polar coordinates:**

r = 137.77 (radius),  $\theta = 5.30699^{\circ}$  (angle) 137.77 result practically equal to the golden angle value 137.5

Or:

```
(([2[((3*(3e+8)^4)/(((8*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2)))^1/3*[-1+sqrt((1-(((((3e+8)^4)/(((9*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))^1/3]]))^1/6 - 8 - 0.47
```

#### Input interpretation:

$$\left( 2 \left[ \sqrt[3]{\frac{3 (3 \times 10^8)^4}{(8 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}} \right] \right) \right)$$

$$\sqrt[3]{-1 + \sqrt{1 - \frac{(3 \times 10^8)^4}{(9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}} } \right)$$

$$(1/6) - 8 - 0.47$$

#### **Result:**

137.182... + 12.7429... i

#### **Polar coordinates:**

r = 137.773 (radius),  $\theta = 5.307^{\circ}$  (angle) 137.773 result practically equal to the golden angle value 137.5

#### and:

 $(([2[((3*(3e+8)^4)/(((8*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2)))^1/3*[-1+sqrt((1-(((((3e+8)^4)/(((9*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))^1/3]]))^1/6-7$ 

# Input interpretation:

$$\left( 2 \left[ \sqrt[3]{\frac{3 (3 \times 10^8)^4}{(8 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}} \right] \right)$$

$$\sqrt[3]{-1 + \sqrt{1 - \frac{(3 \times 10^8)^4}{(9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2}} \right)$$

$$(1/6) - 7$$

#### **Result:**

138.652... + 12.7429... i

# **Polar coordinates:**

r = 139.237 (radius),  $\theta = 5.25105^{\circ}$  (angle) 139.237 result practically equal to the rest mass of Pion meson 139.57 MeV  $(([2[((3*(3e+8)^4)/(((8*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2)))^1/3*[-1+sqrt((1-(((((3e+8)^4)/(((9*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))^1/3]]))^1/6 - 18$ -golden ratio^2

# Input interpretation:

$$\begin{pmatrix} 2 \sqrt[3]{3} \frac{3(3 \times 10^8)^4}{(8 \times 1.1056 \times 10^{-52})(6.6743 \times 10^{-11})^2(13.12806 \times 10^{39})^2} \\ \sqrt[3]{-1 + \sqrt{1 - \frac{(3 \times 10^8)^4}{(9 \times 1.1056 \times 10^{-52})(6.6743 \times 10^{-11})^2(13.12806 \times 10^{39})^2}} \\ \wedge (1/6) - 18 - \phi^2 \end{pmatrix}$$

 $\phi$  is the golden ratio

#### **Result:**

125.034... + 12.7429... i

#### **Polar coordinates:**

r = 125.682 (radius),  $\theta = 5.81923^{\circ}$  (angle) 125.682 result very near to the Higgs boson mass 125.18 GeV

27\*1/2(((([2[((3\*(3e+8)^4)/(((8\*1.1056e-52)\*(6.6743e-11)^2(13.12806e+39)^2)))^1/3\*[-1+sqrt((1-(((((3e+8)^4)/(((9\*1.1056e-52)\*(6.6743e-11)^2(13.12806e+39)^2))))))]^1/3]]))^1/6-18))-Pi

# Input interpretation:

$$27 \times \frac{1}{2} \left( \left( 2 \left( \sqrt[3]{3} \frac{3 (3 \times 10^8)^4}{(8 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2} \right) - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} \right) - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2)} - (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^{-10})^2 + (1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 10^8)^4 / ((9 \times 10^8)^2$$

#### **Result:**

1720.16... + 172.029... i

#### **Polar coordinates:**

r = 1728.74 (radius),  $\theta = 5.71102^{\circ}$  (angle) 1728.74

or:

```
27*1/2(((([2[((3*(3e+8)^4)/(((8*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2)))^1/3*[-1+sqrt((1-(((((3e+8)^4)/(((9*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))]^1/3]]))^1/6-18))-2.71828
```

#### **Input interpretation:**

$$27 \times \frac{1}{2} \left( \left( 2 \left( \frac{3}{\sqrt{3}} \frac{3 (3 \times 10^8)^4}{(8 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2} \right) - (-1 + \sqrt{(1 - (3 \times 10^8)^4 / ((9 \times 1.1056 \times 10^{-52}) (6.6743 \times 10^{-11})^2 (13.12806 \times 10^{39})^2))} \right) \right)$$
$$(1/3) = (1/3) - (1/6) - 18 - 2.71828$$

#### **Result:**

1720.59... + 172.029... i

#### **Polar coordinates:**

r = 1729.17 (radius),  $\theta = 5.70963^{\circ}$  (angle) 1729.17

This result is very near to the mass of candidate glueball  $f_0(1710)$  scalar meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number) Now:

# **Possible closed forms:**

 $\begin{array}{l} 100 \sqrt{299} \approx 1729.161646 \\ -441 \sqrt{2} \ b_4(2) \approx 1729.1753650 \\ \\ \frac{55\,041\,\pi}{100} \approx 1729.164012 \\ \\ \frac{396\,165}{e^2\,\pi^3} \approx 1729.169323 \\ \\ \\ \frac{9\,e^5}{4\,\log^5(2)\log^2(3)} \approx 1729.1740813 \\ \\ e^{3-2/e+2\,e+2/\pi-2\,\pi}\,\pi^{2+e} \approx 1729.1711327 \end{array}$ 

# From

 $\frac{396\,165}{e^2\,\pi^3}\approx 1729.169323$ 

we obtain:

 $\ln(((((396165/(e^2 \pi^3)))-10^3)))^{1/3}-(21+5) 1/10^2+3*1/10^3)$ 

# Input:

$$\sqrt[3]{\log\left(\frac{396\,165}{e^2\,\pi^3}-10^3\right)-(21+5)\times\frac{1}{10^2}+3\times\frac{1}{10^3}}$$

 $\log(x)$  is the natural logarithm

# **Exact result:**

$$\sqrt[3]{\log\left(\frac{396\,165}{e^2\,\pi^3}-1000\right)}-\frac{257}{1000}$$

# **Decimal approximation:**

1.618010344119830694078484452802092842957577828240226732345... 1.6180103441198... result that is a very good approximation to the value of the golden ratio 1,618033988749...

Alternate forms:  

$$\frac{1000 \sqrt[3]{\log(\frac{396165}{e^2 \pi^3} - 1000)} - 257}{1000}$$

$$\sqrt[3]{-2 - 3 \log(\pi) + \log(5 (79233 - 200 e^2 \pi^3))} - \frac{257}{1000}$$

$$\frac{1000 \sqrt[3]{-2 + \log(5) - 3 \log(\pi) + \log(79233 - 200 e^2 \pi^3)} - 257}{1000}$$

Alternative representations:

$$\frac{3}{\sqrt{\log\left(\frac{396\,165}{e^2\,\pi^3}-10^3\right)}-\frac{21+5}{10^2}+\frac{3}{10^3}}=\frac{3}{\sqrt{\log_e\left(-10^3+\frac{396\,165}{e^2\,\pi^3}\right)}-\frac{26}{10^2}+\frac{3}{10^3}}$$
$$\frac{3}{\sqrt{\log\left(\frac{396\,165}{e^2\,\pi^3}-10^3\right)}-\frac{21+5}{10^2}+\frac{3}{10^3}}=\frac{3}{\sqrt{\log(a)\log_e\left(-10^3+\frac{396\,165}{e^2\,\pi^3}\right)}}-\frac{26}{10^2}+\frac{3}{10^3}}$$
$$\frac{3}{\sqrt{\log\left(\frac{396\,165}{e^2\,\pi^3}-10^3\right)}-\frac{21+5}{10^2}+\frac{3}{10^3}}=\frac{3}{\sqrt{-\text{Li}_1\left(1+10^3-\frac{396\,165}{e^2\,\pi^3}\right)}}-\frac{26}{10^2}+\frac{3}{10^3}}$$

# Series representations:

$$\sqrt[3]{\log\left(\frac{396\,165}{e^2\,\pi^3} - 10^3\right)} - \frac{21+5}{10^2} + \frac{3}{10^3} = -\frac{257}{1000} + \sqrt[3]{\log\left(77\left(-13 + \frac{5145}{e^2\,\pi^3}\right)\right)} - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{77\left(-13 + \frac{5145}{e^2\,\pi^3}\right)}\right)^k}{k}$$

$$\frac{\sqrt[3]{\log\left(\frac{396\,165}{e^2\,\pi^3} - 10^3\right) - \frac{21+5}{10^2} + \frac{3}{10^3} = -\frac{257}{1000} + \sqrt[3]{\left(\frac{1000 + \frac{396\,165}{e^2\,\pi^3} - x\right)}{2\pi}\right) + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1000 + \frac{396\,165}{e^2\,\pi^3} - x\right)^k x^{-k}}{k}}{k}}$$
for  $x < 0$ 

$$\frac{\sqrt[3]{\log\left(\frac{396\,165}{e^2\,\pi^3} - 10^3\right) - \frac{21+5}{10^2} + \frac{3}{10^3} = -\frac{257}{1000} + \sqrt[3]{2\,i\,\pi\left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\,\pi}\right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1000 + \frac{396\,165}{e^2\,\pi^3} - z_0\right)^k z_0^{-k}}{k}}{k}}$$

# Integral representations:

$$\sqrt[3]{\log\left(\frac{396\,165}{e^2\,\pi^3}-10^3\right)} - \frac{21+5}{10^2} + \frac{3}{10^3} = -\frac{257}{1000} + \sqrt[3]{\int_1^{-1000+\frac{396\,165}{e^2\,\pi^3}}\frac{1}{t}\,dt$$

$$\sqrt[3]{\log\left(\frac{396\,165}{e^2\,\pi^3} - 10^3\right) - \frac{21+5}{10^2} + \frac{3}{10^3}} = -\frac{257}{1000} + \frac{\sqrt[3]{-i\int_{-i\,\infty+\gamma}^{i\,\infty+\gamma} \frac{\left(-1001+\frac{396\,165}{e^2\,\pi^3}\right)^{-s}\,\Gamma(-s)^2\,\Gamma(1+s)}{\Gamma(1-s)}}{\sqrt[3]{2\,\pi}} \quad \text{for } -1 < \gamma < 0$$

From (46) and (47), we obtain:

$$\begin{split} r_b &= \; \frac{2GM}{c^2} \left[ 1 + \frac{4}{3} \Lambda_{\rm ext} \left( \frac{GM}{c^2} \right)^2 \right] \,, \\ r_c &= \; \sqrt{\frac{3}{\Lambda_{\rm ext}}} \left( 1 - \frac{GM}{c^2} \sqrt{\frac{\Lambda_{\rm ext}}{3}} \right) \,. \end{split}$$

For c = 299792458,  $\Lambda_{ext} = 1.1056e-52$ , G = 6.6743e-11 and M = 13.12806e+39, we obtain:

 $(2*6.6743e-11*13.12806e+39)/(3e+8)^2 * (((((1+4/3*(1.1056e-52)*((6.6743e-11*13.12806e+39)/(3e+8)^2)^2))))$ 

#### **Input interpretation:**

$$\frac{2 \times 6.6743 \times 10^{-11} \times 13.12806 \times 10^{39}}{(3 \times 10^8)^2} \left(1 + \frac{4}{3} \times 1.1056 \times 10^{-52} \left(\frac{6.6743 \times 10^{-11} \times 13.12806 \times 10^{39}}{(3 \times 10^8)^2}\right)^2\right)$$

#### **Result:**

 $1.9471246857333333333333333605389180080414372326847944... \times 10^{13}$  $1.9471246857333...*10^{13}$ 

and:

 $(3/(1.1056e-52))^{1/2}((((1-((6.6743e-11*13.12806e+39)/(3e+8)^2))))*((((1.1056e-52)/3)^{1/2})))$ 

#### Input interpretation:

	3	$(1 6.6743 \times 10^{-11} \times 13.12806 \times 10^{39})$		$1.1056  imes 10^{-52}$
V	$1.1056 \times 10^{-52}$	$(3 \times 10^8)^2$	V	3

#### **Result:**

From the following ratio between the two results, we obtain:

(1.9471246857333333 × 10^13) / (-9.7356234286656666 × 10^12)

#### **Input interpretation:**

 $1.9471246857333333 \times 10^{13}$ 

 $9.7356234286656666 \times 10^{12}$ 

#### **Result:**

 $-2.00000000000020541057433587344391046755537696094607018182\ldots$ 

-2 result equal to the graviton spin with minus sign

From which:

 $(((1.9471246857333333 \times 10^{13}) / (-9.7356234286656666 \times 10^{12})))^{6}$ 

### Input interpretation:

 $\left(-\frac{1.9471246857333333 \times 10^{13}}{9.7356234286656666 \times 10^{12}}\right)^{6}$ 

#### **Result:**

64.000000003943883027249782767178153043267668312361298414...

64

and:

2(((1.9471246857333333 × 10^13) / (-9.7356234286656666 × 10^12)))^6 + 7 + golden ratio^2

#### Input interpretation:

 $2\left(-\frac{1.9471246857333333\times10^{13}}{9.7356234286656666\times10^{12}}\right)^6 + 7 + \phi^2$ 

 $\phi$  is the golden ratio

### **Result:**

137.6180339888288...

137.6180339888288... result practically equal to the golden angle value 137.5

2(((1.9471246857333333 × 10^13) / (-9.7356234286656666 × 10^12)))^6 + 7 + golden ratio^3

#### Input interpretation:

 $2\left(-\frac{1.9471246857333333\times10^{13}}{9.7356234286656666\times10^{12}}\right)^{6}+7+\phi^{3}$ 

 $\phi$  is the golden ratio

#### **Result:**

139.2360679775787...

139.2360679775787... result practically equal to the rest mass of Pion meson 139.57  $\,\mathrm{MeV}$ 

2(((1.9471246857333333 × 10^13) / (-9.7356234286656666 × 10^12)))^6 - Pi + 1/golden ratio

Input interpretation:  $2\left(-\frac{1.947124685733333\times10^{13}}{9.7356234286656666\times10^{12}}\right)^{6} - \pi + \frac{1}{\phi}$ 

∅ is the golden ratio

#### **Result:**

125.4764413352390...

125.476441335239... result very near to the Higgs boson mass 125.18 GeV

27\*(((((1.9471246857333333 × 10^13) / (-9.7356234286656666 × 10^12)))^6))+1

#### Input interpretation:

 $27 \left(-\frac{1.9471246857333333 \times 10^{13}}{9.7356234286656666 \times 10^{12}}\right)^6 + 1$ 

#### **Result:**

1729.00000001064848417357441347138101321682270444337550571... 1729

This result is very near to the mass of candidate glueball  $f_0(1710)$  scalar meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross-Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

and again:

((((27\*(((((1.94712468573 × 10^13) / (-9.73562342866 × 10^12)))^6))+1))))^1/15 -(21+5) 1/10^3

Input interpretation:

 $15\sqrt{27\left(-\frac{1.94712468573\times10^{13}}{9.73562342866\times10^{12}}\right)^6+1} - (21+5)\times\frac{1}{10^3}$ 

#### **Result:**

 $1.617815228748053139601228337209585701809813539180470570595\ldots$ 

1.6178152287... result that is a very good approximation to the value of the golden ratio 1,618033988749...

#### We have also that dividing:

$$\frac{\frac{2 \times 6.6743 \times 10^{-11} \times 13.12806 \times 10^{39}}{(3 \times 10^8)^2}}{\left(1 + \frac{4}{3} \times 1.1056 \times 10^{-52} \left(\frac{6.6743 \times 10^{-11} \times 13.12806 \times 10^{39}}{(3 \times 10^8)^2}\right)^2\right)}$$

 $1.94712468573333333333333333605389180080414372326847944...\times10^{13}$ 

by

$$\sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \\ \sqrt[3]{-1 - \sqrt{1 - \frac{299\,792\,458^4}{(9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} }$$

 $r = 4.8776 \times 10^{12}$  (radius),  $\theta = -30.^{\circ}$  (angle)

#### we obtain:

 $\begin{array}{l} (1.9471246857333e+13) / \left[ ((((((3*299792458^4)/(((8*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))^{1/3} * ((-1+sqrt((((1-((((299792458^4)/(((9*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))))^{1/3} \right] \\ \end{array}$ 

#### Input interpretation:

 $\left(1.9471246857333 \times 10^{13}\right) \Big/$ 

$$\begin{pmatrix} \sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \\ \sqrt[3]{-1 + \sqrt{1 - \frac{299\,792\,458^4}{(9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \end{pmatrix}$$

#### **Result:**

3.45715... – 1.99599... i

### **Polar coordinates:**

r = 3.99197 (radius),  $\theta = -30.^{\circ}$  (angle) 3.99197

#### And dividing:

$$\sqrt{\frac{3}{1.1056 \times 10^{-52}}} \left( \left( 1 - \frac{6.6743 \times 10^{-11} \times 13.12806 \times 10^{39}}{(3 \times 10^8)^2} \right) \sqrt{\frac{1.1056 \times 10^{-52}}{3}} \right)$$

by

$$\sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}} \\ \sqrt[3]{-1 - \sqrt{1 - \frac{299\,792\,458^4}{(9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}}}$$

$$r = 4.8776 \times 10^{12}$$
 (radius),  $\theta = -30.^{\circ}$  (angle)

we obtain:

$$(-9.7356234286656e+12)/[(((((((3*299792458^4)/(((8*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))^1/3*((-1+sqrt((((1-((((299792458^4)/(((9*1.1056e-52)*(6.6743e-11)^2(13.12806e+39)^2))))))))^1/3]$$

# Input interpretation:

$$-\left[\left(9.7356234286656 \times 10^{12}\right)\right] \\ \left[\sqrt[3]{\frac{3 \times 299\,792\,458^4}{(8 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}}\right] \\ \sqrt[3]{-1 + \sqrt{1 - \frac{299\,792\,458^4}{(9 \times 1.1056 \times 10^{-52})\,(6.6743 \times 10^{-11})^2\,(13.12806 \times 10^{39})^2}}}\right]$$

#### **Result:**

- 1.72858... + 0.997993... i

#### **Polar coordinates:**

r = 1.99599 (radius),  $\theta = 150.^{\circ}$  (angle) 1.99599  $\approx 2$  result practically equal to the graviton spin

From the difference between the two results, we obtain:

(3.99197-1.99599)

#### Input interpretation:

3.99197 - 1.99599

#### **Result:**

1.99598

1.99598

# Possible closed forms:

 $\sqrt{\frac{247}{62}} \approx 1.995963668$  $\log\left(\frac{1}{2}\left(6\ e + e^2 + (\pi - 6)\ \pi\right)\right) \approx 1.995978105$ 

From the result of the difference (closed form)

$$\log\left(\frac{1}{2}\left(6\ e + e^2 + (\pi - 6)\ \pi\right)\right) \approx 1.995978105$$

we obtain:

$$2(((\log(1/2 (6 e + e^{2} + (\pi - 6) \pi)))))^{6-1})$$

#### Input:

 $2\log^6 \left(\frac{1}{2} \left(6 \ e + e^2 + (\pi - 6) \ \pi\right)\right) - 1$ 

log(x) is the natural logarithm

# **Decimal approximation:**

125.4633359511961552446188043526188035573296255814272482170...

### 125.46333595... result very near to the Higgs boson mass 125.18 GeV

# Alternate forms:

$$2 \log^{6} \left(\frac{1}{2} \left(e \left(6+e\right)+\left(\pi-6\right)\pi\right)\right) - 1$$
  
$$2 \left(\log \left(6 e+e^{2}+\left(\pi-6\right)\pi\right)-\log (2)\right)^{6} - 1$$
  
$$-1 + 2 \log^{6} (2) + 2 \log^{6} \left(6 e+e^{2}-6 \pi+\pi^{2}\right) - 12 \log^{5} (2) \log \left(6 e+e^{2}-6 \pi+\pi^{2}\right) - 12 \log (2) \log^{5} \left(6 e+e^{2}-6 \pi+\pi^{2}\right) - 40 \log^{3} (2) \log^{3} \left(6 e+e^{2}-6 \pi+\pi^{2}\right) + 30 \log^{4} (2) \log^{2} \left(6 e+e^{2}-6 \pi+\pi^{2}\right) + 30 \log^{2} (2) \log^{4} \left(6 e+e^{2}-6 \pi+\pi^{2}\right)$$

# Alternative representations:

$$2 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) - 1 = -1 + 2 \log^{6} \left(\frac{1}{2} \left(6 e + (-6 + \pi) \pi + e^{2}\right)\right)$$
$$2 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) - 1 = -1 + 2 \left(\log(a) \log_{a} \left(\frac{1}{2} \left(6 e + (-6 + \pi) \pi + e^{2}\right)\right)\right)^{6}$$
$$2 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) - 1 = -1 + 2 \left(-\text{Li}_{1} \left(1 + \frac{1}{2} \left(-6 e - (-6 + \pi) \pi - e^{2}\right)\right)\right)^{6}$$

# Series representations:

$$2 \log^{6} \left( \frac{1}{2} \left( 6 e + e^{2} + (\pi - 6) \pi \right) \right) - 1 = -1 + 2 \left( \log \left( -1 + \frac{1}{2} \left( 6 e + e^{2} + (-6 + \pi) \pi \right) \right) - \sum_{k=1}^{\infty} \frac{\left( -\frac{2}{-2 + 6 e + e^{2} - 6 \pi + \pi^{2}} \right)^{k}}{k} \right)^{6}$$

$$2 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) - 1 = -1 + 2 \left(2 i \pi \left[\frac{\arg\left(\frac{1}{2} \left(6 e + e^{2} + (-6 + \pi) \pi\right) - x\right)}{2 \pi}\right] + \log(x) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k} \left(6 e + e^{2} + (-6 + \pi) \pi - 2 x\right)^{k} x^{-k}}{k} \right)^{6} \text{ for } x < 0$$

$$2\log^{6}\left(\frac{1}{2}\left(6\ e+e^{2}+(\pi-6)\ \pi\right)\right)-1 = -1+2\left(2\ i\ \pi\left\lfloor\frac{\pi-\arg\left(\frac{1}{z_{0}}\right)-\arg(z_{0})}{2\ \pi}\right\rfloor+\log(z_{0})-\sum_{k=1}^{\infty}\frac{\left(-\frac{1}{2}\right)^{k}\left(6\ e+e^{2}+(-6+\pi)\ \pi-2\ z_{0}\right)^{k}\ z_{0}^{-k}}{k}\right)^{6}$$

### **Integral representations:**

$$2\log^{6}\left(\frac{1}{2}\left(6\,e+e^{2}+(\pi-6)\,\pi\right)\right)-1=-1+2\left(\int_{1}^{\frac{1}{2}\left(6\,e+e^{2}+(-6+\pi)\pi\right)}\frac{1}{t}\,dt\right)^{6}$$

$$2\log^{6}\left(\frac{1}{2}\left(6\ e+e^{2}+(\pi-6)\ \pi\right)\right)-1=-1-\frac{\left(\int_{-i\ \infty+\gamma}^{i\ \infty+\gamma}\frac{\left(-1+\frac{1}{2}\left(6\ e+e^{2}+(-6+\pi)\ \pi\right)\right)^{-s}\ \Gamma(-s)^{2}\ \Gamma(1+s)}{\Gamma(1-s)}\ d\ s\right)^{6}}{32\ \pi^{6}}$$
for  $-1<\gamma<0$ 

and:

 $2(((\log(1/2 (6 e + e^{2} + (\pi - 6) \pi))))^{6+1})$ 

**Input:**  $2 \log^{6} \left( \frac{1}{2} \left( 6 e + e^{2} + (\pi - 6) \pi \right) \right) + 11$ 

log(x) is the natural logarithm

#### **Decimal approximation:**

137.4633359511961552446188043526188035573296255814272482170...

137.46333595... result practically equal to the golden angle value 137.5

**Alternate forms:** 

 $11 + 2\log^6\left(\frac{1}{2}\left(e\left(6 + e\right) + (\pi - 6)\pi\right)\right)$ 

 $11 + 2 \left( \log (6 \ e + e^2 + (\pi - 6) \ \pi ) - \log(2) \right)^6$ 

$$\begin{aligned} &11 + 2\log^{6}(2) + 2\log^{6}(6\ e + e^{2} - 6\ \pi + \pi^{2}) - 12\log^{5}(2)\log(6\ e + e^{2} - 6\ \pi + \pi^{2}) - \\ &12\log(2)\log^{5}(6\ e + e^{2} - 6\ \pi + \pi^{2}) - 40\log^{3}(2)\log^{3}(6\ e + e^{2} - 6\ \pi + \pi^{2}) + \\ &30\log^{4}(2)\log^{2}(6\ e + e^{2} - 6\ \pi + \pi^{2}) + 30\log^{2}(2)\log^{4}(6\ e + e^{2} - 6\ \pi + \pi^{2}) \end{aligned}$$

# Alternative representations:

$$2 \log^{6} \left(\frac{1}{2} \left(6 \ e + e^{2} + (\pi - 6) \ \pi\right)\right) + 11 = 11 + 2 \log^{6} \left(\frac{1}{2} \left(6 \ e + (-6 + \pi) \ \pi + e^{2}\right)\right)$$
$$2 \log^{6} \left(\frac{1}{2} \left(6 \ e + e^{2} + (\pi - 6) \ \pi\right)\right) + 11 = 11 + 2 \left(\log(a) \log_{a} \left(\frac{1}{2} \left(6 \ e + (-6 + \pi) \ \pi + e^{2}\right)\right)\right)^{6}$$
$$2 \log^{6} \left(\frac{1}{2} \left(6 \ e + e^{2} + (\pi - 6) \ \pi\right)\right) + 11 = 11 + 2 \left(-\text{Li}_{1} \left(1 + \frac{1}{2} \left(-6 \ e - (-6 + \pi) \ \pi - e^{2}\right)\right)\right)^{6}$$

# Series representations:

$$2\log^{6}\left(\frac{1}{2}\left(6\ e+e^{2}+(\pi-6)\ \pi\right)\right)+11=$$

$$11+2\left(\log\left(-1+\frac{1}{2}\left(6\ e+e^{2}+(-6+\pi)\ \pi\right)\right)-\sum_{k=1}^{\infty}\frac{\left(-\frac{2}{-2+6\ e+e^{2}-6\ \pi+\pi^{2}}\right)^{k}}{k}\right)^{6}$$

$$2 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + 11 =$$

$$11 + 2 \left(2 i \pi \left[\frac{\arg\left(\frac{1}{2} \left(6 e + e^{2} + (-6 + \pi) \pi\right) - x\right)}{2 \pi}\right] + \log(x) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k} \left(6 e + e^{2} + (-6 + \pi) \pi - 2 x\right)^{k} x^{-k}}{k}\right)^{6} \text{ for } x < 0$$

$$2\log^{6}\left(\frac{1}{2}\left(6\ e+e^{2}+(\pi-6)\ \pi\right)\right)+11 = 11+2\left(2\ i\ \pi\left[\frac{\pi-\arg\left(\frac{1}{z_{0}}\right)-\arg(z_{0})}{2\ \pi}\right]+\log(z_{0})-\sum_{k=1}^{\infty}\frac{\left(-\frac{1}{2}\right)^{k}\left(6\ e+e^{2}+(-6+\pi)\ \pi-2\ z_{0}\right)^{k}\ z_{0}^{-k}}{k}\right)^{6}$$

# Integral representations:

$$2\log^{6}\left(\frac{1}{2}\left(6e+e^{2}+(\pi-6)\pi\right)\right)+11=11+2\left(\int_{1}^{\frac{1}{2}\left(6e+e^{2}+(-6+\pi)\pi\right)}\frac{1}{t}\,dt\right)^{6}$$

$$2\log^{6}\left(\frac{1}{2}\left(6\ e+e^{2}+(\pi-6)\ \pi\right)\right)+11=11-\frac{\left(\int_{-i\ \infty+\gamma}^{i\ \infty+\gamma}\frac{\left(-1+\frac{1}{2}\left(6\ e+e^{2}+(-6+\pi)\ \pi\right)\right)^{-s}\ \Gamma(-s)^{2}\ \Gamma(1+s)}{\Gamma(1-s)}\ d\ s\right)^{6}}{32\ \pi^{6}}$$
for  $-1<\gamma<0$ 

$$2(((\log(1/2 (6 e + e^{2} + (\pi - 6) \pi))))^{6+13})))$$

**Input:**  $2 \log^{6} \left( \frac{1}{2} \left( 6 e + e^{2} + (\pi - 6) \pi \right) \right) + 13$ 

log(x) is the natural logarithm

### **Decimal approximation:**

139.4633359511961552446188043526188035573296255814272482170...

139.46333595... result practically equal to the rest mass of Pion meson 139.57 MeV

# Alternate forms:

$$\begin{aligned} &13 + 2 \log^{6} \left(\frac{1}{2} \left(e \left(6 + e\right) + \left(\pi - 6\right) \pi\right)\right) \\ &13 + 2 \left(\log\left(6 \ e + e^{2} + \left(\pi - 6\right) \pi\right) - \log(2)\right)^{6} \\ &13 + 2 \log^{6}(2) + 2 \log^{6}(6 \ e + e^{2} - 6 \ \pi + \pi^{2}) - 12 \log^{5}(2) \log(6 \ e + e^{2} - 6 \ \pi + \pi^{2}) - 12 \log^{2}(2) \log^{3}(6 \ e + e^{2} - 6 \ \pi + \pi^{2}) + 12 \log(2) \log^{5}(6 \ e + e^{2} - 6 \ \pi + \pi^{2}) - 40 \log^{3}(2) \log^{3}(6 \ e + e^{2} - 6 \ \pi + \pi^{2}) + 30 \log^{4}(2) \log^{2}(6 \ e + e^{2} - 6 \ \pi + \pi^{2}) + 30 \log^{2}(2) \log^{4}(6 \ e + e^{2} - 6 \ \pi + \pi^{2}) \end{aligned}$$

# Alternative representations:

$$2 \log^{6} \left(\frac{1}{2} \left(6 \ e + e^{2} + (\pi - 6) \ \pi\right)\right) + 13 = 13 + 2 \log^{6} \left(\frac{1}{2} \left(6 \ e + (-6 + \pi) \ \pi + e^{2}\right)\right)$$
$$2 \log^{6} \left(\frac{1}{2} \left(6 \ e + e^{2} + (\pi - 6) \ \pi\right)\right) + 13 = 13 + 2 \left(\log(a) \log_{a} \left(\frac{1}{2} \left(6 \ e + (-6 + \pi) \ \pi + e^{2}\right)\right)\right)^{6}$$
$$2 \log^{6} \left(\frac{1}{2} \left(6 \ e + e^{2} + (\pi - 6) \ \pi\right)\right) + 13 = 13 + 2 \left(-\text{Li}_{1} \left(1 + \frac{1}{2} \left(-6 \ e - (-6 + \pi) \ \pi - e^{2}\right)\right)\right)^{6}$$

# Series representations:

$$2 \log^{6} \left( \frac{1}{2} \left( 6 e + e^{2} + (\pi - 6) \pi \right) \right) + 13 =$$
  
$$13 + 2 \left( \log \left( -1 + \frac{1}{2} \left( 6 e + e^{2} + (-6 + \pi) \pi \right) \right) - \sum_{k=1}^{\infty} \frac{\left( -\frac{2}{-2 + 6 e + e^{2} - 6 \pi + \pi^{2}} \right)^{k}}{k} \right)^{6}$$

$$2 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + 13 =$$

$$13 + 2 \left(2 i \pi \left[\frac{\arg\left(\frac{1}{2} \left(6 e + e^{2} + (-6 + \pi) \pi\right) - x\right)}{2 \pi}\right] + \log(x) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k} \left(6 e + e^{2} + (-6 + \pi) \pi - 2 x\right)^{k} x^{-k}}{k} \right)^{6} \text{ for } x < 0$$

$$2\log^{6}\left(\frac{1}{2}\left(6\ e+e^{2}+(\pi-6)\ \pi\right)\right)+13=13+2\left(2\ i\ \pi\left[\frac{\pi-\arg\left(\frac{1}{z_{0}}\right)-\arg(z_{0})}{2\ \pi}\right]\right)+\log(z_{0})-\sum_{k=1}^{\infty}\frac{\left(-\frac{1}{2}\right)^{k}\left(6\ e+e^{2}+(-6+\pi)\ \pi-2\ z_{0}\right)^{k}\ z_{0}^{-k}}{k}\right)^{6}$$

# Integral representations:

$$2\log^{6}\left(\frac{1}{2}\left(6\ e + e^{2} + (\pi - 6)\ \pi\right)\right) + 13 = 13 + 2\left(\int_{1}^{\frac{1}{2}\left(6\ e + e^{2} + (-6+\pi)\ \pi\right)}\frac{1}{t}\ dt\right)^{6}$$
$$\left(\int_{1}^{t}\frac{(e^{2}+e^{2})^{2}}{(e^{2}+e^{2})^{2}}\left(\frac{(e^{2}+e^{2})^{2}}{(e^{2}+e^{2})^{2}}\right)^{-s}\Gamma(-s)^{2}\Gamma(-s$$

$$2 \log^{6} \left(\frac{1}{2} \left(6 \ e + e^{2} + (\pi - 6) \ \pi\right)\right) + 13 = 13 - \frac{\left(\int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{\left(-1 + \frac{1}{2} \left(6 \ e + e^{2} + (-6 + \pi) \ \pi\right)\right)^{-s} \ \Gamma(-s)^{2} \ \Gamma(1+s)}{\Gamma(1-s)} \ ds\right)^{6}}{32 \ \pi^{6}}$$
for  $-1 < \gamma < 0$ 

$$27*(((\log(1/2 (6 e + e^{2} + (\pi - 6) \pi)))))^{6} + (21+Pi-golden ratio^{2}+1/4)$$

**Input:** 27 log<sup>6</sup>  $\left(\frac{1}{2} \left(6 e + e^2 + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^2 + \frac{1}{4}\right)$ 

log(x) is the natural logarithm

# Exact result:

$$-\phi^{2} + \frac{85}{4} + \pi + 27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right)$$

#### **Decimal approximation:**

 $1729.028594005987994192611915309267712790426805568837193889\ldots$ 

#### 1729.028594005...

This result is very near to the mass of candidate glueball  $f_0(1710)$  scalar meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

# Alternate forms: $-\phi^{2} + \frac{85}{4} + \pi + 27 \log^{6} \left(\frac{1}{2} \left(e \left(6 + e\right) + (\pi - 6) \pi\right)\right)$ $\frac{79}{4} - \frac{\sqrt{5}}{2} + \pi + 27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right)$ $\frac{1}{4} \left(79 - 2 \sqrt{5}\right) + \pi + 27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right)$

#### **Alternative representations:**

$$27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) = 21 + \pi + \frac{1}{4} - \phi^{2} + 27 \log^{6} \left(\frac{1}{2} \left(6 e + (-6 + \pi) \pi + e^{2}\right)\right)$$

$$27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) = 21 + \pi + \frac{1}{4} - \phi^{2} + 27 \left(\log(a) \log_{a} \left(\frac{1}{2} \left(6 e + (-6 + \pi) \pi + e^{2}\right)\right)\right)^{6}$$

$$27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) = 21 + \pi + \frac{1}{4} - \phi^{2} + 27 \left(-\text{Li}_{1} \left(1 + \frac{1}{2} \left(-6 e - (-6 + \pi) \pi - e^{2}\right)\right)\right)^{6}$$

# Series representations:

$$27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) = \frac{85}{4} - \phi^{2} + \pi + 27 \left(\log\left(-1 + \frac{1}{2} \left(6 e + e^{2} + (-6 + \pi) \pi\right)\right) - \sum_{k=1}^{\infty} \frac{\left(-\frac{2}{-2 + 6 e + e^{2} - 6 \pi + \pi^{2}}\right)^{k}}{k}\right)^{6}$$

$$27 \log^{6} \left(\frac{1}{2} \left(6 \ e + e^{2} + (\pi - 6) \ \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) = \frac{85}{4} - \phi^{2} + \pi + 27 \left[2 \ i \ \pi \left[\frac{\arg\left(\frac{1}{2} \left(6 \ e + e^{2} + (-6 + \pi) \ \pi\right) - x\right)}{2 \ \pi}\right] + \log(x) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k} \left(6 \ e + e^{2} + (-6 + \pi) \ \pi - 2 \ x\right)^{k} \ x^{-k}}{k}\right)^{6} \text{ for } x < 0$$

$$27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) = \frac{85}{4} - \phi^{2} + \pi + 27 \left[2 i \pi \left[\frac{\pi - \arg\left(\frac{1}{z_{0}}\right) - \arg(z_{0})}{2 \pi}\right] + \log(z_{0}) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{2}\right)^{k} \left(6 e + e^{2} + (-6 + \pi) \pi - 2 z_{0}\right)^{k} z_{0}^{-k}}{k}\right]^{6}$$

# Integral representations:

$$27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) = \frac{85}{4} - \phi^{2} + \pi + 27 \left(\int_{1}^{\frac{1}{2}(6 e + e^{2} + (-6 + \pi)\pi)} \frac{1}{t} dt\right)^{6}$$

$$27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) = \frac{85}{4} - \phi^{2} + \pi - \frac{27 \left(\int_{-i \ \infty + \gamma}^{i \ \infty + \gamma} \frac{\left(-1 + \frac{1}{2} \left(6 e + e^{2} + (-6 + \pi)\pi\right)\right)^{-s} \Gamma(-s)^{2} \Gamma(1+s)}{\Gamma(1-s)} ds\right)^{6}}{64 \pi^{6}} \quad \text{for } -1 < \gamma < 0$$

((((27\*(((log(1/2 (6 e + e^2 + ( $\pi$  - 6)  $\pi$ )))))^6+(21+Pi-golden ratio^2+1/4)))))^1/15-(29-3) 1/10^3

#### Input:

$$\sqrt[15]{27 \log^6 \left(\frac{1}{2} \left(6 \ e + e^2 + (\pi - 6) \ \pi\right)\right)} + \left(21 + \pi - \phi^2 + \frac{1}{4}\right) - (29 - 3) \times \frac{1}{10^3}$$

log(x) is the natural logarithm

 $\phi$  is the golden ratio

#### **Exact result:**

$$\sqrt[15]{-\phi^2 + \frac{85}{4} + \pi + 27\log^6\left(\frac{1}{2}\left(6\ e + e^2 + (\pi - 6)\ \pi\right)\right)} - \frac{13}{500}$$

#### **Decimal approximation:**

 $1.617817041083401032228911515905750743175142696031835014892\ldots$ 

1.61781704108... result that is a very good approximation to the value of the golden ratio 1,618033988749...

#### Alternate forms:

$$\begin{split} & \frac{15}{\sqrt{-\phi^2} + \frac{85}{4} + \pi + 27\log^6 \left(\frac{1}{2}\left(e\left(6 + e\right) + (\pi - 6)\pi\right)\right) - \frac{13}{500}} \\ & \frac{15}{\sqrt{\frac{1}{4}\left(79 - 2\sqrt{5}\right) + \pi + 27\log^6 \left(\frac{1}{2}\left(6e + e^2 + (\pi - 6)\pi\right)\right)} - \frac{13}{500}} \\ & \frac{15}{\sqrt{\frac{85}{4} - \frac{1}{4}\left(1 + \sqrt{5}\right)^2 + \pi + 27\log^6 \left(\frac{1}{2}\left(6e + e^2 + (\pi - 6)\pi\right)\right)} - \frac{13}{500}} \end{split}$$

#### Alternative representations:

$$\sqrt[15]{27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right) - \frac{29 - 3}{10^{3}} = -\frac{26}{10^{3}} + \sqrt[15]{21 + \pi} + \frac{1}{4} - \phi^{2} + 27 \log^{6}_{e} \left(\frac{1}{2} \left(6 e + (-6 + \pi) \pi + e^{2}\right)\right) }$$

$$\sqrt[15]{27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right)} - \frac{29 - 3}{10^{3}} = -\frac{26}{10^{3}} + \sqrt[15]{21 + \pi} + \frac{1}{4} - \phi^{2} + 27 \left(\log(a) \log_{a} \left(\frac{1}{2} \left(6 e + (-6 + \pi) \pi + e^{2}\right)\right)\right)^{6}}$$

$$\sqrt[15]{27 \log^{6} \left(\frac{1}{2} \left(6 e + e^{2} + (\pi - 6) \pi\right)\right) + \left(21 + \pi - \phi^{2} + \frac{1}{4}\right)} - \frac{29 - 3}{10^{3}} = -\frac{26}{10^{3}} + \sqrt[15]{21 + \pi} + \frac{1}{4} - \phi^{2} + 27 \left(-\text{Li}_{1} \left(1 + \frac{1}{2} \left(-6 e - (-6 + \pi) \pi - e^{2}\right)\right)\right)^{6} }$$

# Series representations:

$$\begin{split} & \sqrt[15]{27 \log^6 \left(\frac{1}{2} \left(6 \ e + e^2 + (\pi - 6) \ \pi\right)\right) + \left(21 + \pi - \phi^2 + \frac{1}{4}\right) - \frac{29 - 3}{10^3} = \\ & -\frac{13}{500} + \left(\frac{85}{4} - \frac{1}{4} \left(1 + \sqrt{5}\right)^2 + \pi + \\ & 27 \left(\log \left(-1 + \frac{1}{2} \left(6 \ e + e^2 + (-6 + \pi) \ \pi\right)\right) - \sum_{k=1}^{\infty} \frac{\left(-\frac{2}{-2 + 6 \ e + e^2 - 6 \ \pi + \pi^2}\right)^k}{k}\right)^6\right) \land (1/15) \end{split}$$

$$\begin{split} & \sqrt[15]{27 \log^6 \left(\frac{1}{2} \left(6 \ e + e^2 + (\pi - 6) \ \pi\right)\right) + \left(21 + \pi - \phi^2 + \frac{1}{4}\right) - \frac{29 - 3}{10^3} = -\frac{13}{500} + \\ & \left(\frac{85}{4} - \frac{1}{4} \left(1 + \sqrt{5}\right)^2 + \pi + 27 \left(2 \ i \ \pi \left[\frac{\arg\left(\frac{1}{2} \left(6 \ e + e^2 + (-6 + \pi) \ \pi\right) - x\right)}{2 \ \pi}\right]\right] + \log(x) - \\ & \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(6 \ e + e^2 + (-6 + \pi) \ \pi - 2 \ x\right)^k \ x^{-k}}{k} \right)^6}{k} \right)^{-1/15} \text{ for } x < 0 \end{split}$$

$$\begin{split} & \sqrt[15]{27 \log^6 \left(\frac{1}{2} \left(6 \ e + e^2 + (\pi - 6) \ \pi\right)\right) + \left(21 + \pi - \phi^2 + \frac{1}{4}\right)} - \frac{29 - 3}{10^3} = \\ & -\frac{13}{500} + \left(\frac{85}{4} - \frac{1}{4} \left(1 + \sqrt{5}\right)^2 + \pi + 27 \left(2 \ i \ \pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2 \ \pi}\right]\right] + \log(z_0) - \\ & \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(6 \ e + e^2 + (-6 + \pi) \ \pi - 2 \ z_0\right)^k \ z_0^{-k}}{k} \right)^6}{2 \ n - \frac{1}{10} \right) \\ & = \frac{100}{2} \left(\frac{1}{2} \left(1 + \sqrt{5}\right)^2 + \frac{1}{2} \left(1 + \sqrt{5}\right)$$

# Integral representations:

$$\frac{15\sqrt{27\log^6\left(\frac{1}{2}\left(6\ e+e^2+(\pi-6)\ \pi\right)\right)}+\left(21+\pi-\phi^2+\frac{1}{4}\right)-\frac{29-3}{10^3}}{10^3}= -\frac{13}{500}+\frac{15\sqrt{\frac{85}{4}}-\frac{1}{4}\left(1+\sqrt{5}\right)^2+\pi+27\left(\int_1^{\frac{1}{2}\left(6\ e+e^2+(-6+\pi)\pi\right)}\frac{1}{t}\ dt\right)^6}{10^3}$$

$$\begin{split} & \frac{15\sqrt{27\log^6\left(\frac{1}{2}\left(6\ e+e^2+(\pi-6)\ \pi\right)\right)+\left(21+\pi-\phi^2+\frac{1}{4}\right)}}{-\frac{10^3}{10^3}} = \\ & -\frac{13}{500}+\frac{15\sqrt{\frac{85}{4}-\frac{1}{4}\left(1+\sqrt{5}\ \right)^2+\pi-\frac{27\left(\int_{-i\ \infty+\gamma}^{i\ \infty+\gamma}\frac{\left(\frac{2}{-2+6\ e+e^2+(-6+\pi)\ \pi}\right)^s\ \Gamma(-s)^2\ \Gamma(1+s)}{\Gamma(1-s)}\ ds\right)^6}{64\ \pi^6} \end{split}$$

We note that, from the following integral representation, we obtain:

-13/500 + (85/4 - (1 + Sqrt[5])^2/4 + Pi + 27 Integrate[t^(-1), {t, 1, (6 E + E^2 + (-6 + Pi) Pi)/2}]^6)^(1/15)

Input:

$$-\frac{13}{500} + \sqrt[15]{\frac{85}{4} - \frac{1}{4}\left(1 + \sqrt{5}\right)^2 + \pi + 27\left(\int_1^{\frac{1}{2}\left(6e + e^2 + (-6+\pi)\pi\right)}\frac{1}{t} dt\right)^6}$$

#### **Result:**

$$\sqrt[15]{\frac{85}{4} - \frac{1}{4}\left(1 + \sqrt{5}\right)^2 + \pi + 27\left(\log\left(6\,e + e^2 + (\pi - 6)\,\pi\right) - \log(2)\right)^6} - \frac{13}{500} \approx 1.61782$$

1.61782 result that is a very good approximation to the value of the golden ratio 1,618033988749...

**Computation result:** 

$$-\frac{13}{500} + \frac{15}{\sqrt{4}} \left\{ \frac{85}{4} - \frac{1}{4} \left( 1 + \sqrt{5} \right)^2 + \pi + 27 \left( \int_1^{\frac{1}{2} \left( 6e + e^2 + (-6+\pi)\pi \right)} \frac{1}{t} dt \right)^6 = \frac{15\sqrt{85}}{\sqrt{4}} - \frac{1}{4} \left( 1 + \sqrt{5} \right)^2 + \pi + 27 \left( \log \left( 6e + e^2 + (\pi - 6)\pi \right) - \log(2) \right)^6 - \frac{13}{500} = \frac{13}$$

#### Alternate forms:

$$15\sqrt{\frac{79}{4} - \frac{\sqrt{5}}{2}} + \pi + 27\log^6\left(\frac{2}{e(6+e) + (\pi-6)\pi}\right) - \frac{13}{500}$$
$$15\sqrt{\frac{79}{4} - \frac{\sqrt{5}}{2}} + \pi + 27\log^6\left(\frac{2}{6e+e^2 + (\pi-6)\pi}\right) - \frac{13}{500}$$

$$\sqrt[15]{\frac{1}{4} \left(79 - 2\sqrt{5}\right) + \pi + 27 \left(\log(6 e + e^2 + (\pi - 6)\pi) - \log(2)\right)^6} - \frac{13}{500}$$

From:

#### TRANSACTIONS OF THE AMERICAN MATHEMATICAL SOCIETY Volume 349, Number 6, June 1997, Pages 2125 {2173 S 0002-9947(97)01738-8 **RAMANUJAN'S CLASS INVARIANTS, KRONECKER'S LIMIT FORMULA, AND MODULAR EQUATIONS** -*BRUCE C. BERNDT, HENG HUAT CHAN, AND LIANG - CHENG ZHANG*

We have that:

RAMANUJAN'S CLASS INVARIANTS

2149

Theorem 5.4.

$$\begin{split} G_{553} &= \left(\sqrt{\frac{100+11\sqrt{79}}{4}} + \sqrt{\frac{96+11\sqrt{79}}{4}}\right)^{1/2} \\ &\times \left(\sqrt{\frac{143+16\sqrt{79}}{2}} + \sqrt{\frac{141+16\sqrt{79}}{2}}\right)^{1/2}. \end{split}$$

From:

$$G_{553} = \left(\sqrt{\frac{100 + 11\sqrt{79}}{4}} + \sqrt{\frac{96 + 11\sqrt{79}}{4}}\right)^{1/2} \\ \times \left(\sqrt{\frac{143 + 16\sqrt{79}}{2}} + \sqrt{\frac{141 + 16\sqrt{79}}{2}}\right)^{1/2}$$

We note that:

141 - 4 = 137; 141 - 2 = 139; 141 - 7 = 134; 143 - 18 = 125; 143 - 4 = 139;143 - 76 - 3 = 64; 143 - 11 - 4 = 128 Now, we have:

Input:  

$$\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}$$

$$\sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)}$$

Result:  

$$\sqrt{\left(\left(\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}\right)\right)} \\
\left(\sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} + \sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}\right)}$$

#### **Decimal approximation:**

18.26422315928407823493115977083140400145481154893144639087...

18.264223159284...

#### Alternate forms:

$$\frac{1}{4} \sqrt{\left(2\sqrt{96+11\sqrt{79}} + 11\sqrt{2} + \sqrt{158}\right) \left(\sqrt{2\left(141+16\sqrt{79}\right)} + 8\sqrt{2} + \sqrt{158}\right) 2} \sqrt{\frac{1}{100} + 11\sqrt{79} + 138x^{6} + 496x^{5} + 127x^{4} + 496x^{3} + 138x^{2} - 334x + 1}{100} + 11x^{79} + \sqrt{100} + 11\sqrt{79} + \sqrt{143} + 16\sqrt{79} + \sqrt{143} + 16\sqrt{79} + \sqrt{143} + 16\sqrt{79} + 2^{3/4}}$$

#### Minimal polynomial:

 $x^{16} - 334 x^{14} + 138 x^{12} + 496 x^{10} + 127 x^8 + 496 x^6 + 138 x^4 - 334 x^2 + 1$ 

From which, we obtain:

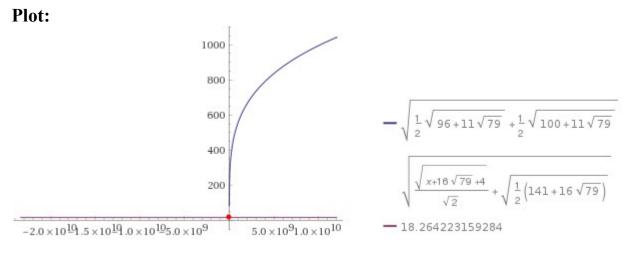
 $sqrt(((((((1/4(100+11sqrt79)))^{1/2} + ((1/4(96+11sqrt79)))^{1/2}))))) * sqrt(((((((1/2((x+4)+16sqrt79)))^{1/2} + ((1/2(141+16sqrt79)))^{1/2}))))) = 18.264223159284$ 

#### Input interpretation:

$$\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}$$
$$\sqrt{\sqrt{\frac{1}{2}\left((x+4)+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} = 18.264223159284$$

**Result:** 

$$\sqrt{\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}} = 18.264223159284$$



#### Solution:

x = 139.000000000

#### 139 result very near to the rest mass of Pion meson 139.57 MeV

 $sqrt(((((((1/4(100+11sqrt79)))^{1/2} + ((1/4(96+11sqrt79)))^{1/2}))))) * sqrt(((((((1/2(143+16sqrt79)))^{1/2} + ((1/2((x+4)+16sqrt79)))^{1/2}))))) = 18.264223159284$ 

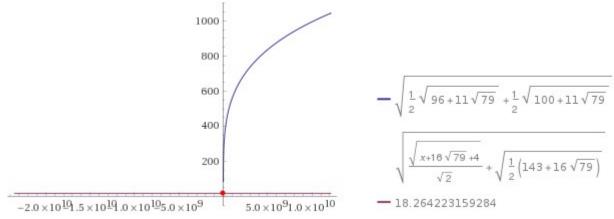
#### Input interpretation:

$$\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} } } \sqrt{\sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left((x+4)+16\sqrt{79}\right)} } = 18.264223159284$$

**Result:** 

$$\sqrt{\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}} = 18.264223159284$$

**Plot:** 



#### Solution:

x = 137.0000000000

137 result very near to the golden angle value 137.5

 $sqrt(((((((1/4(100+11sqrt79)))^{1/2} + ((1/4(96+11sqrt79)))^{1/2}))))) * sqrt(((((((1/2((x+18)+16sqrt79)))^{1/2} + ((1/2(141+16sqrt79)))^{1/2}))))) = 18.264223159284$ 

#### Input interpretation:

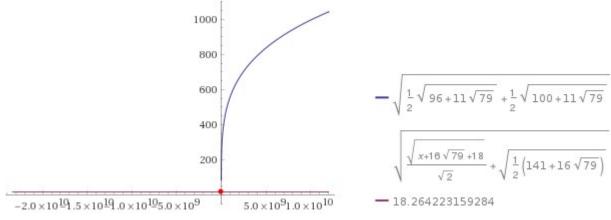
$$\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}$$

$$\sqrt{\sqrt{\frac{1}{2}\left((x+18)+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} = 18.264223159284$$

**Result:** 

$$\sqrt{\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}} = 18.264223159284$$

**Plot:** 



#### Solution:

x = 125.0000000000

### 125 result very near to the Higgs boson mass 125.18 GeV

 $sqrt(((((((1/4(100+11sqrt79)))^{1/2} + ((1/4(96+11sqrt79)))^{1/2}))))) * sqrt(((((((1/2((x+11+4)+16sqrt79)))^{1/2} + ((1/2(141+16sqrt79)))^{1/2}))))) = 18.264223159284$ 

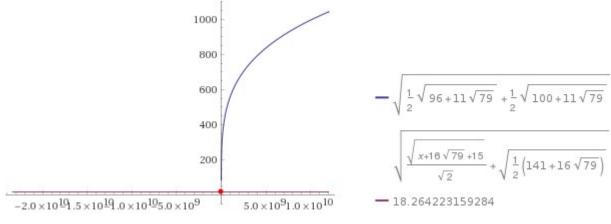
### Input interpretation:

$$\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}$$
$$\sqrt{\sqrt{\frac{1}{2}\left((x+11+4)+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} = 18.264223159284$$

**Result:** 

$$\sqrt{\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}} = 18.264223159284$$

**Plot:** 



#### Solution:

x = 128.0000000000

128 = 64\*2

$$24*4*sqrt((((((1/4(100+11sqrt79)))^{1/2} + ((1/4(96+11sqrt79)))^{1/2})))) * sqrt((((((1/2(143+16sqrt79)))^{1/2} + ((1/2(141+16sqrt79)))^{1/2})))) -24$$

Input:

$$24 \times 4\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}}{\sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)}} - 24$$

**Result:** 

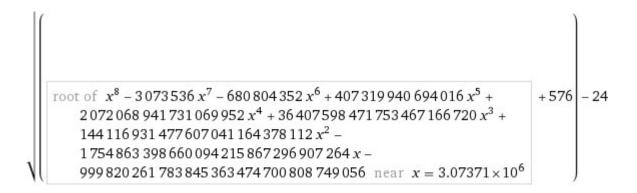
$$96 \sqrt{\left(\left(\frac{1}{2}\sqrt{96+11\sqrt{79}}+\frac{1}{2}\sqrt{100+11\sqrt{79}}\right)\right)} \left(\sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)}+\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}\right)\right)-24}$$

#### **Decimal approximation:**

1729.365423291271510553391337999814784139661908697418853524... 1729.3654232912...

This result is very near to the mass of candidate glueball  $f_0(1710)$  scalar meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

# Alternate forms: 24 $\left(\sqrt{2\left(2\sqrt{96+11\sqrt{79}}+11\sqrt{2}+\sqrt{158}\right)}\left(\sqrt{2\left(141+16\sqrt{79}\right)}+8\sqrt{2}+\sqrt{158}\right)}\right)$ $-1\right)$ $24\left(2\sqrt[4]{2}\sqrt{\left(\left(\sqrt{96+11\sqrt{79}}+\sqrt{100+11\sqrt{79}}\right)}\right)$ $\left(\sqrt{141+16\sqrt{79}}+\sqrt{143+16\sqrt{79}}\right)\right)$ $-1\right)$



#### Minimal polynomial:

 $x^{16}$  + 384  $x^{15}$  - 3 009 024  $x^{14}$  - 1 026 514 944  $x^{13}$  -149 019 181 056  $x^{12}$  - 12 078 599 897 088  $x^{11}$  - 186 912 469 942 272  $x^{10}$  + 79 809 519 474 966 528  $x^{9}$  + 11 139 400 543 229 706 240  $x^{8}$  + 845 455 300 038 330 679 296  $x^{7}$  + 75 854 671 334 524 185 477 120  $x^{6}$  + 6 263 097 910 682 549 175 189 504  $x^{5}$  + 406 765 656 037 755 285 651 062 784  $x^{4}$  + 17 861 614 552 038 435 392 682 196 992  $x^{3}$  -1 422 817 988 535 687 593 024 569 737 216  $x^{2}$  -84 233 443 135 684 522 361 630 251 548 672 x -999 820 261 783 845 363 474 700 808 749 056

Note that the previous obtained results 3.99197 and 1.99599 can be calculate also as follows:

Input:

$$\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} } } \sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} \times \frac{1}{\pi^2} - \pi + 5 + \frac{10\pi}{144 - (21+8) - 2^2} }$$

**Result:** 

$$5 + \frac{1}{\pi^2} \left( \sqrt{\left( \left( \frac{1}{2} \sqrt{96 + 11\sqrt{79}} + \frac{1}{2} \sqrt{100 + 11\sqrt{79}} \right) \right)} \right) \left( \sqrt{\frac{1}{2} \left( 141 + 16\sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 143 + 16\sqrt{79} \right)} \right) \right) - \frac{101\pi}{111}$$

# **Decimal approximation:**

3.991986420404937063776120654524447454564967851921287091550... 3.99198642...

Property:  

$$5 + \frac{1}{\pi^2} \left( \sqrt{\left( \left( \frac{1}{2} \sqrt{96 + 11 \sqrt{79}} + \frac{1}{2} \sqrt{100 + 11 \sqrt{79}} \right) \right)} \right) \left( \sqrt{\frac{1}{2} \left( 141 + 16 \sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 143 + 16 \sqrt{79} \right)} \right) \frac{101 \pi}{111} \text{ is a transcendental number}}$$

#### Alternate forms:

$$\frac{1}{444 \pi^2} \left( 111 \sqrt{\left( 2 \left( 2 \sqrt{96 + 11 \sqrt{79}} + 11 \sqrt{2} + \sqrt{158} \right) \right)} \right) \left( \sqrt{2 \left( 141 + 16 \sqrt{79} \right)} + 8 \sqrt{2} + \sqrt{158} \right) - 404 \pi^3 + 2220 \pi^2 \right)$$

$$\sqrt{ \begin{bmatrix} \operatorname{root of } x^8 - 334 x^7 + 138 x^6 + 496 x^5 + 127 x^4 + 496 x^3 + 138 x^2 - 334 x + 1 \\ \operatorname{near } x = 333.582 \end{bmatrix} + \frac{\pi^2}{5 - \frac{101 \pi}{111}} + \frac{\pi^2}{222 \pi^2} \left[ 111 \sqrt[4]{2} \sqrt{\left( \sqrt{96 + 11 \sqrt{79}} + \sqrt{100 + 11 \sqrt{79}} \right) \left( \sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}} \right) + 1110 \pi^2 - 202 \pi^3 \right] }$$

Series representations:

$$\begin{split} \frac{1}{\pi^2} \sqrt{\sqrt{\frac{1}{4} \left(100 + 11\sqrt{79}\right)} + \sqrt{\frac{1}{4} \left(96 + 11\sqrt{79}\right)}} \\ \sqrt{\sqrt{\frac{1}{2} \left(143 + 16\sqrt{79}\right)} + \sqrt{\frac{1}{2} \left(141 + 16\sqrt{79}\right)} - \pi + 5 + \frac{10\pi}{144 - (21 + 8) - 2^2} = \\ -\frac{1}{111\pi^2} \left( -555\pi^2 + 101\pi^3 - 111\sqrt{-1} + \frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}} \right) \\ \sqrt{-1} + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} \\ \sum_{k_1 = 0}^{\infty} \sum_{k_2 = 0}^{\infty} \left(\frac{1}{2}\right) \left(\frac{1}{k_2}\right) \left(-1 + \frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}}\right)^{-k_1} \\ \left(-1 + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}}\right)^{-k_2} \right) \\ \frac{1}{\pi^2} \sqrt{\sqrt{\frac{1}{4} \left(100 + 11\sqrt{79}\right)} + \sqrt{\frac{1}{4} \left(96 + 11\sqrt{79}\right)}} \\ \sqrt{\sqrt{\frac{1}{2} \left(143 + 16\sqrt{79}\right)} + \sqrt{\frac{1}{2} \left(141 + 16\sqrt{79}\right)} - \pi + 5 + \frac{10\pi}{144 - (21 + 8) - 2^2} = \\ -\frac{1}{111\pi^2} \left( -555\pi^2 + 101\pi^3 - 111\sqrt{-1} + \frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}} \right) \\ \sqrt{-1} + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} \sum_{k_1 = 0}^{\infty} \sum_{k_2 = 0}^{\infty} \frac{1}{k_1! k_2!} \left(-1)^{k_1 + k_2} \\ \left(-\frac{1}{2})_{k_1} \left(-\frac{1}{2})_{k_2} \left(-1 + \frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}} \right)^{-k_1} \\ \left(-1 + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} \right)^{-k_2} \right) \end{split}$$

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$$\begin{aligned} \frac{1}{\pi^2} \sqrt{\sqrt{\frac{1}{4} \left(100 + 11\sqrt{79}\right)} + \sqrt{\frac{1}{4} \left(96 + 11\sqrt{79}\right)}} \\ \sqrt{\sqrt{\frac{1}{2} \left(143 + 16\sqrt{79}\right)} + \sqrt{\frac{1}{2} \left(141 + 16\sqrt{79}\right)} - \pi + 5 + \frac{10\pi}{144 - (21 + 8) - 2^2} = \\ -\frac{1}{111\pi^2} \left( -555\pi^2 + 101\pi^3 - 111\sqrt{z_0}^2 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{1}{k_1! k_2!} (-1)^{k_1+k_2} \left(-\frac{1}{2}\right)_{k_1} \\ \left(-\frac{1}{2}\right)_{k_2} \left(\frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}} - z_0\right)^{k_1} \\ \left(\frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} - z_0\right)^{k_2} z_0^{-k_1-k_2} \right) \\ \text{for not} \left( \left(z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \le 0 \right) \right) \end{aligned}$$

and:

Input:  

$$\frac{1}{2} \left( \sqrt{\sqrt{\frac{1}{4} \left( 100 + 11\sqrt{79} \right)}} + \sqrt{\frac{1}{4} \left( 96 + 11\sqrt{79} \right)} \right) \\ \sqrt{\sqrt{\frac{1}{2} \left( 143 + 16\sqrt{79} \right)}} + \sqrt{\frac{1}{2} \left( 141 + 16\sqrt{79} \right)} \times \frac{1}{\pi^2} - \pi + 5 + \frac{10\pi}{144 - (21 + 8) - 2^2} \right)$$

**Result:** 

$$\frac{1}{2} \left( 5 + \frac{1}{\pi^2} \left( \sqrt{\left( \left( \frac{1}{2} \sqrt{96 + 11\sqrt{79}} + \frac{1}{2} \sqrt{100 + 11\sqrt{79}} \right) \right) \right)} \right) \left( \sqrt{\frac{1}{2} \left( 141 + 16\sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 143 + 16\sqrt{79} \right)} \right) \right) - \frac{101\pi}{111} \right)$$

# **Decimal approximation:**

1.995993210202468531888060327262223727282483925960643545775...

#### 1.9959932102024...

Property:  

$$\frac{1}{2} \left( 5 + \frac{1}{\pi^2} \left( \sqrt{\left( \left( \frac{1}{2} \sqrt{96 + 11 \sqrt{79}} + \frac{1}{2} \sqrt{100 + 11 \sqrt{79}} \right) \right) \right) \left( \sqrt{\frac{1}{2} \left( 141 + 16 \sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 143 + 16 \sqrt{79} \right)} \right) \right) \right) - \frac{101 \pi}{111} \right)$$
is a transcendental number

Alternate forms:

$$\frac{1}{888 \pi^2} \left( 111 \sqrt{\left( 2 \left( 2 \sqrt{96 + 11 \sqrt{79}} + 11 \sqrt{2} + \sqrt{158} \right) \right)} \right)} \left( \sqrt{2 \left( 141 + 16 \sqrt{79} \right)} + 8 \sqrt{2} + \sqrt{158} \right) - 404 \pi^3 + 2220 \pi^2 \right)$$

$$\frac{1}{2} \left( \frac{\sqrt{1000 \text{ f } x^8 - 334 x^7 + 138 x^6 + 496 x^5 + 127 x^4 + 496 x^3 + 138 x^2 - 334 x + 1}{1000 \text{ near } x = 333.582} + \frac{1}{\pi^2} \right) \right)$$

$$\frac{1}{444 \pi^2} \left( 111 \frac{\pi}{\sqrt{2}} + \frac{111 \sqrt{2}}{\sqrt{\left(\sqrt{96 + 11 \sqrt{79}} + \sqrt{100 + 11 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right)}}{\sqrt{141 + 16 \sqrt{79}} + 1110 \pi^2 - 202 \pi^3} \right)$$

Series representations:

$$\begin{split} \frac{1}{2} \left( \frac{1}{\pi^2} \sqrt{\sqrt{\frac{1}{4} \left( 100 + 11\sqrt{79} \right)} + \sqrt{\frac{1}{4} \left( 96 + 11\sqrt{79} \right)} \right)} \\ \sqrt{\sqrt{\frac{1}{2} \left( 143 + 16\sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 141 + 16\sqrt{79} \right)} - \frac{1}{\pi + 5} + \frac{10\pi}{144 - (21 + 8) - 2^2} \right) = -\frac{1}{222\pi^2} \\ \left( -555\pi^2 + 101\pi^3 - 111\sqrt{-1 + \frac{1}{2}}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}} \right) \\ \sqrt{-1 + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} \\ \sqrt{-1 + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}} \right)^{k_1} \\ \left( -1 + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} \right)^{k_2} \right) \\ \frac{1}{2} \left( \frac{1}{\pi^2} \sqrt{\sqrt{\frac{1}{4} \left( 100 + 11\sqrt{79} \right)}} + \sqrt{\frac{1}{4} \left( 96 + 11\sqrt{79} \right)} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} \right)^{k_2} \right) \\ \sqrt{\sqrt{\frac{1}{2} \left( 143 + 16\sqrt{79} \right)}} + \sqrt{\frac{1}{4} \left( 96 + 11\sqrt{79} \right)} \\ \sqrt{\sqrt{\frac{1}{2} \left( 143 + 16\sqrt{79} \right)}} + \sqrt{\frac{1}{2} \left( 141 + 16\sqrt{79} \right)} - \pi + 5 + \frac{10\pi}{144 - (21 + 8) - 2^2} \right) = -\frac{1}{222\pi^2} \\ \left( -555\pi^2 + 101\pi^3 - 111\sqrt{-1 + \frac{1}{2} \sqrt{96 + 11\sqrt{79}}} + \frac{1}{2} \sqrt{100 + 11\sqrt{79}} \right) \\ \sqrt{-1 + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} \right) \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{1}{k_1!k_2!} \left( -1 \right)^{k_1+k_2} \\ \left( -\frac{1}{2} \right)^{k_1} \left( -\frac{1}{2} \right)^{k_2} \left( -1 + \frac{1}{2} \sqrt{96 + 11\sqrt{79}} + \frac{1}{2} \sqrt{100 + 11\sqrt{79}} \right)^{k_1} \\ \left( -1 + \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} \right)^{k_2} \right) \end{split}$$

$$\begin{split} \frac{1}{2} \left( \frac{1}{\pi^2} \sqrt{\sqrt{\frac{1}{4} \left( 100 + 11\sqrt{79} \right)} + \sqrt{\frac{1}{4} \left( 96 + 11\sqrt{79} \right)}} \right)} \\ \sqrt{\sqrt{\frac{1}{2} \left( 143 + 16\sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 141 + 16\sqrt{79} \right)}} \\ - \pi + 5 + \frac{10\pi}{144 - (21 + 8) - 2^2} \right) = \\ - \frac{1}{222\pi^2} \left( -555\pi^2 + 101\pi^3 - 111\sqrt{z_0}^2 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{1}{k_1! k_2!} (-1)^{k_1+k_2} \left( -\frac{1}{2} \right)_{k_1} \\ \left( -\frac{1}{2} \right)_{k_2} \left( \frac{1}{2} \sqrt{96 + 11\sqrt{79}} + \frac{1}{2} \sqrt{100 + 11\sqrt{79}} - z_0 \right)^{k_1} \\ \left( \frac{\sqrt{141 + 16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143 + 16\sqrt{79}}}{\sqrt{2}} - z_0 \right)^{k_2} z_0^{-k_1-k_2} \right) \end{split}$$

for not  $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \le 0))$ 

We have also:

Input:

$$\left( \sqrt{\sqrt{\frac{1}{4} \left( 100 + 11 \sqrt{79} \right)}} + \sqrt{\frac{1}{4} \left( 96 + 11 \sqrt{79} \right)} \right)$$
$$\sqrt{\sqrt{\frac{1}{2} \left( 143 + 16 \sqrt{79} \right)}} + \sqrt{\frac{1}{2} \left( 141 + 16 \sqrt{79} \right)} \right) \times 7 - \phi^{2}$$

 $\phi$  is the golden ratio

Result:  $7 \sqrt{\left(\left(\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}\right) + \left(\sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} + \sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}\right)\right)} - \phi^2$ 

#### **Decimal approximation:**

 $125.2315281262386527963135315614541898924633716627143618740\ldots$ 

#### 125.23152812... result very near to the Higgs boson mass 125.18 GeV

#### **Alternate forms:**

$$\frac{1}{4} \left( 7 \sqrt{\left( 2 \left( 2 \sqrt{96 + 11 \sqrt{79}} + 11 \sqrt{2} + \sqrt{158} \right) \right)} \right) \left( \sqrt{2 \left( 141 + 16 \sqrt{79} \right)} + 8 \sqrt{2} + \sqrt{158} \right) - 2 \sqrt{5} - 6 \right)$$

$$-\frac{3}{2} - \frac{\sqrt{5}}{2} + \frac{7\sqrt{(\sqrt{96 + 11\sqrt{79}} + \sqrt{100 + 11\sqrt{79}})(\sqrt{141 + 16\sqrt{79}} + \sqrt{143 + 16\sqrt{79}})}{2^{3/4}}$$

$$\frac{1}{2} \left( -3 - \sqrt{5} + 7\sqrt[4]{2} \sqrt{\left( \left( \sqrt{96 + 11\sqrt{79}} + \sqrt{100 + 11\sqrt{79}} \right) \right) \right)} \right)$$
$$\left( \sqrt{141 + 16\sqrt{79}} + \sqrt{143 + 16\sqrt{79}} \right) \right)$$

#### **Minimal polynomial:**

 $x^{32} + 48 x^{31} - 31636 x^{30} - 1457100 x^{29} + 237166742 x^{28} +$  $10\,852\,454\,928\,x^{27}+208\,860\,647\,870\,x^{26}+2\,337\,693\,848\,412\,x^{25}+$  $14\,775\,812\,816\,990\,x^{24}$  + 6 307 193 998 080  $x^{23}$  - 996 322 876 073 062  $x^{22}$  - $12564289768747956x^{21} - 95663943751479376x^{20} -$ 546 657 809 493 104 400  $x^{19}$  – 2 667 680 177 341 822 618  $x^{18}$  – 12 737 292 429 118 825 908  $x^{17}$  – 40 304 890 833 149 917 147  $x^{16}$  +  $249\,786\,177\,215\,940\,781\,104\,x^{15}+5\,862\,929\,052\,424\,482\,294\,722\,x^{14}+$  $58\,105\,016\,393\,009\,246\,507\,616\,x^{13}+377\,241\,781\,521\,632\,616\,442\,154\,x^{12}+$  $1\,717\,214\,912\,105\,840\,646\,352\,272\,x^{11}+4\,765\,105\,784\,230\,154\,872\,703\,300\,x^{10}+$  $624\,025\,314\,623\,628\,992\,038\,296\,x^9$  - 129765910557785247105213188 $x^8$  - $1119302309232351909211629552x^7 -$ 6 278 500 908 795 317 168 727 094 320 x<sup>6</sup> -24 873 269 293 786 680 872 257 459 104 x<sup>5</sup> -11751902441974234930156182576x<sup>4</sup> + 212 792 483 072 384 314 482 547 751 040 x<sup>3</sup> +  $472465687895454912557715860544x^{2}$  + 238 353 981 758 302 812 406 312 748 544 x - 309 925 067 387 877 390 106 459 584 Series representations:

$$7\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}} = \sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} = \phi^{2} = -\phi^{2} + 7\sqrt{-1+\frac{1}{2}\sqrt{96+11\sqrt{79}}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}} = \sqrt{-1+\frac{1}{2}\sqrt{96+11\sqrt{79}}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}}}{\sqrt{2}} = \sum_{k_{1}=0}^{\infty}\sum_{k_{2}=0}^{\infty} \left(\frac{1}{2}\\k_{1}\right)\left(\frac{1}{2}\\k_{2}\right)\left(-1+\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}\right)^{-k_{1}} = \left(-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}}\right)^{-k_{2}}$$

$$\begin{aligned} & 7\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} \\ & \sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} - \phi^2 = \\ & -\phi^2 + 7\sqrt{-1+\frac{1}{2}\sqrt{96+11\sqrt{79}}} + \frac{1}{2}\sqrt{100+11\sqrt{79}} \\ & \sqrt{-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}} \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{1}{k_1!k_2!} (-1)^{k_1+k_2} \\ & \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \left(-1+\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}\right)^{-k_1} \\ & \left(-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}}\right)^{-k_2} \end{aligned}$$

$$\begin{aligned} 7\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} \\ \sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} & -\phi^2 = \\ -\phi^2 + 7\sqrt{z_0}^2 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{1}{k_1!k_2!} (-1)^{k_1+k_2} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \\ \left(\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}} - z_0\right)^{k_1} \\ \left(\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}} - z_0\right)^{k_2} z_0^{-k_1-k_2} \\ \text{for not} \left(\left(z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \le 0\right)\right) \end{aligned}$$

Input:

$$\begin{pmatrix} \sqrt{\frac{1}{4} \left(100 + 11\sqrt{79}\right)} + \sqrt{\frac{1}{4} \left(96 + 11\sqrt{79}\right)} \\ \sqrt{\sqrt{\frac{1}{2} \left(143 + 16\sqrt{79}\right)}} + \sqrt{\frac{1}{2} \left(141 + 16\sqrt{79}\right)} \end{pmatrix} \times 7 + 7 + \pi - \frac{1}{\phi}$$

 $\phi$  is the golden ratio

**Result:** 

$$\begin{aligned} &-\frac{1}{\phi} + 7 + 7 \sqrt{\left(\left(\frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}}\right)\right)} \\ & \left(\sqrt{\frac{1}{2}\left(141 + 16\sqrt{79}\right)} + \sqrt{\frac{1}{2}\left(143 + 16\sqrt{79}\right)}\right)\right) + \pi \end{aligned}$$

#### **Decimal approximation:**

137.3731207798284460347761749447336927766605410620894676949...

137.3731207798... result practically equal to the golden angle value 137.5

Property:  

$$7 + 7 \sqrt{\left(\left(\frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}}\right)\right)}$$

$$\left(\sqrt{\frac{1}{2}\left(141 + 16\sqrt{79}\right)} + \sqrt{\frac{1}{2}\left(143 + 16\sqrt{79}\right)}\right) - \frac{1}{\phi} + \pi \text{ is a transcendental number}$$

Alternate forms:

$$\begin{split} \frac{1}{4} \left( 7 \sqrt{\left( 2 \left( 2 \sqrt{96 + 11 \sqrt{79}} + 11 \sqrt{2} + \sqrt{158} \right) \right)} \\ \left( \sqrt{2 \left( 141 + 16 \sqrt{79} \right)} + 8 \sqrt{2} + \sqrt{158} \right) \right) - 2 \sqrt{5} + 4 \pi + 30 \right) \\ 7 - \frac{2}{1 + \sqrt{5}} + 7 \sqrt{\left( \left( \frac{1}{2} \left( \frac{11}{\sqrt{2}} + \sqrt{\frac{79}{2}} \right) + \frac{1}{2} \sqrt{96 + 11 \sqrt{79}} \right) \\ \left( \sqrt{\frac{1}{2} \left( 141 + 16 \sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 143 + 16 \sqrt{79} \right)} \right) \right) + \pi \\ - \frac{1}{\phi} + 7 + \frac{1}{2 \sqrt[4]{2}} 7 \sqrt{\left( \left( 11 + \sqrt{79} + \sqrt{96 - 7i \sqrt{7}} + \sqrt{i \left( 7 \sqrt{7} + -96 i \right)} \right) \\ \left( \sqrt{141 - 7i \sqrt{7}} + 2 \left( 4 \sqrt{2} + \sqrt{\frac{79}{2}} + \frac{1}{2} \sqrt{i \left( 7 \sqrt{7} + -141 i \right)} \right) \right) \right) + \pi \end{split}$$

Series representations:

$$\begin{aligned} & 7\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} \\ & \sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} + 7 + \pi - \frac{1}{\phi} = \\ & \frac{1}{\phi} \left(-1+7\phi+\phi\pi+7\phi\sqrt{-1+\frac{1}{2}\sqrt{96+11\sqrt{79}}} + \frac{1}{2}\sqrt{100+11\sqrt{79}} \right) \\ & \sqrt{-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}} \\ & \sqrt{-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}} \\ & \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \left(\frac{1}{2}\right) \left(\frac{1}{2} \\ & k_2\right) \left(-1+\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}\right)^{-k_1} \\ & \left(-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}}\right)^{-k_2} \end{aligned}$$

$$\begin{aligned} & 7\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}} \\ & \sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} + 7 + \pi - \frac{1}{\phi} =} \\ & \frac{1}{\phi} \left(-1+7\phi+\phi\pi+7\phi\sqrt{-1+\frac{1}{2}\sqrt{96+11\sqrt{79}}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}}{\sqrt{2}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}} \right) \\ & \sqrt{-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}} \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{1}{k_1!k_2!} (-1)^{k_1+k_2}}{\left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \left(-1+\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}\right)^{-k_1}}{\left(-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}}\right)^{-k_2}} \end{aligned}$$

$$7\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} + 7 + \pi - \frac{1}{\phi} = \frac{1}{\phi}\left(-1+7\phi+\phi\pi+7\phi\sqrt{z_0}^2\sum_{k_1=0}^{\infty}\sum_{k_2=0}^{\infty}\frac{1}{k_1!k_2!}(-1)^{k_1+k_2}\left(-\frac{1}{2}\right)_{k_1}\left(-\frac{1}{2}\right)_{k_2} + \left(\frac{1}{2}\sqrt{96+11\sqrt{79}}\right)^2 + \frac{1}{2}\sqrt{100+11\sqrt{79}} - z_0\right)^{k_1} + \left(\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}} - z_0\right)^{k_2}z_0^{-k_1-k_2}$$

for not  $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \le 0))$ 

(((sqrt(((((((1/4(100+11sqrt79)))^1/2 + ((1/4(96+11sqrt79)))^1/2))))) \* sqrt((((((((1/2(143+16sqrt79)))^1/2 + ((1/2(141+16sqrt79)))^1/2)))))))\*7+11+1/golden ratio

Input:  

$$\left(\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}\right)$$

$$\sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)}\right) \times 7 + 11 + \frac{1}{\phi}$$

 $\phi$  is the golden ratio

# **Result:**

$$\frac{1}{\phi} + 11 + 7 \sqrt{\left( \left( \frac{1}{2} \sqrt{96 + 11 \sqrt{79}} + \frac{1}{2} \sqrt{100 + 11 \sqrt{79}} \right) \right) } \left( \sqrt{\frac{1}{2} \left( 141 + 16 \sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 143 + 16 \sqrt{79} \right)} \right)$$

# **Decimal approximation:**

139.4675961037384424927227052301854661279039900223258875982...

139.4675961... result practically equal to the rest mass of Pion meson 139.57 MeV

# Alternate forms:

$$\begin{split} \frac{1}{4} \left( 7 \sqrt{\left( 2 \left( 2 \sqrt{96 + 11 \sqrt{79}} + 11 \sqrt{2} + \sqrt{158} \right) \right)} \\ \left( \sqrt{2 \left( 141 + 16 \sqrt{79} \right)} + 8 \sqrt{2} + \sqrt{158} \right) \right) + 2 \sqrt{5} + 42 \right) \\ \frac{1}{\frac{1}{2} + \frac{\sqrt{5}}{2}} + \frac{1}{2} \left( 22 + 7 \sqrt[4]{2} \sqrt{\left( \left( \sqrt{96 + 11 \sqrt{79}} + \sqrt{100 + 11 \sqrt{79}} \right) \right)} \\ \left( \sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}} \right) \right) \right) \\ 11 + \frac{2}{1 + \sqrt{5}} + 7 \sqrt{\left( \left( \frac{1}{2} \left( \frac{11}{\sqrt{2}} + \sqrt{\frac{79}{2}} \right) + \frac{1}{2} \sqrt{96 + 11 \sqrt{79}} \right)} \\ \left( \sqrt{\frac{1}{2} \left( 141 + 16 \sqrt{79} \right)} + \sqrt{\frac{1}{2} \left( 143 + 16 \sqrt{79} \right)} \right) \right) \end{split}$$

# Series representations:

$$7\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} + 11 + \frac{1}{\phi} = \frac{1}{\sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} + \frac{1}{2}\sqrt{100+11\sqrt{79}}} + \frac{1}{\phi} + \frac{1$$

$$\begin{aligned} & 7\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)}} \\ & \sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)}} + 11 + \frac{1}{\phi} = \\ & \frac{1}{\phi} \left(1+11\phi+7\phi\sqrt{-1+\frac{1}{2}\sqrt{96+11\sqrt{79}}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}} \right) \\ & \sqrt{-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}}}{\sqrt{2}} \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \frac{1}{k_1!k_2!} (-1)^{k_1+k_2} \\ & \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \left(-1+\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}}\right)^{-k_1} \\ & \left(-1+\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}}\right)^{-k_2} \right) \end{aligned}$$

$$\begin{aligned} 7\sqrt{\sqrt{\frac{1}{4}\left(100+11\sqrt{79}\right)}} + \sqrt{\frac{1}{4}\left(96+11\sqrt{79}\right)} \\ \sqrt{\sqrt{\frac{1}{2}\left(143+16\sqrt{79}\right)}} + \sqrt{\frac{1}{2}\left(141+16\sqrt{79}\right)} + 11 + \frac{1}{\phi} = \\ \frac{1}{\phi}\left(1+11\phi+7\phi\sqrt{z_0}^2\sum_{k_1=0}^{\infty}\sum_{k_2=0}^{\infty}\frac{1}{k_1!k_2!}\left(-1\right)^{k_1+k_2}\left(-\frac{1}{2}\right)_{k_1}\left(-\frac{1}{2}\right)_{k_2} \\ \left(\frac{1}{2}\sqrt{96+11\sqrt{79}} + \frac{1}{2}\sqrt{100+11\sqrt{79}} - z_0\right)^{k_1} \\ \left(\frac{\sqrt{141+16\sqrt{79}}}{\sqrt{2}} + \frac{\sqrt{143+16\sqrt{79}}}{\sqrt{2}} - z_0\right)^{k_2}z_0^{-k_1-k_2} \end{aligned}$$

for not  $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \le 0))$ 

Input:

$$27 \times \frac{1}{2} \left[ \left( \sqrt{\sqrt{\frac{1}{4} \left( 100 + 11\sqrt{79} \right)} + \sqrt{\frac{1}{4} \left( 96 + 11\sqrt{79} \right)}} \right) + \sqrt{\frac{1}{2} \left( 141 + 16\sqrt{79} \right)} \right] \times 7 \right] + 3$$

#### **Result:**

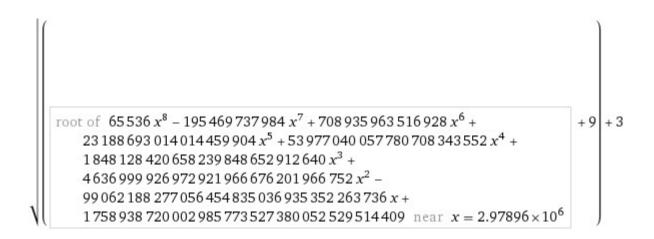
$$3 + \frac{189}{2} \sqrt{\left(\left(\frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}}\right)\right)} \\ \left(\sqrt{\frac{1}{2}\left(141 + 16\sqrt{79}\right)} + \sqrt{\frac{1}{2}\left(143 + 16\sqrt{79}\right)}\right)\right)}$$

## **Decimal approximation:**

 $1728.969088552345393200994598343567678137479691374021683937... \\ 1728.969088... \approx 1729$ 

This result is very near to the mass of candidate glueball  $f_0(1710)$  scalar meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross– Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729 (taxicab number)

Alternate forms:  $\frac{3}{8} \left[ 63 \sqrt{\left[ 2 \left( 2 \sqrt{96 + 11 \sqrt{79}} + 11 \sqrt{2} + \sqrt{158} \right) \right]} \left( \sqrt{2 \left( 141 + 16 \sqrt{79} \right)} + 8 \sqrt{2} + \sqrt{158} \right) \right] + 8 \right]} \\
\frac{3}{4} \left[ 4 + 63 \sqrt[4]{2} \sqrt{\left[ \left( \sqrt{96 + 11 \sqrt{79}} + \sqrt{100 + 11 \sqrt{79}} \right) \right]} \left( \sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}} \right) \right] \right]}$ 



#### **Minimal polynomial:**

 $\begin{array}{l} 65\,536\,x^{16}-3\,145\,728\,x^{15}-195\,403\,677\,696\,x^{14}+\\ 8\,208\,936\,271\,872\,x^{13}+561\,166\,787\,026\,944\,x^{12}-\\ 24\,043\,972\,005\,494\,784\,x^{11}+23\,562\,652\,012\,612\,780\,032\,x^{10}-\\ 698\,691\,474\,503\,260\,176\,384\,x^{9}+62\,338\,687\,419\,214\,090\,632\,960\,x^{8}-\\ 1\,345\,569\,559\,694\,305\,507\,141\,632\,x^{7}+1\,859\,937\,757\,117\,567\,609\,201\,090\,560\,x^{6}-\\ 33\,313\,128\,049\,735\,116\,784\,201\,469\,952\,x^{5}+\\ 4\,836\,667\,750\,647\,926\,754\,128\,729\,775\,264\,x^{4}-\\ 56\,043\,194\,862\,537\,243\,407\,423\,452\,731\,264\,x^{3}-\\ 98\,895\,256\,279\,685\,429\,644\,236\,592\,081\,460\,664\,x^{2}+\\ 594\,373\,129\,662\,338\,729\,010\,221\,612\,113\,582\,416\,x+\\ 1\,758\,938\,720\,002\,985\,773\,527\,380\,052\,529\,514\,409 \end{array}$ 

$$\begin{cases} 27 \times \frac{1}{2} \left( \left( \sqrt{\frac{1}{4} \left( 100 + 11\sqrt{79} \right)} + \sqrt{\frac{1}{4} \left( 96 + 11\sqrt{79} \right)} \right) \\ \sqrt{\sqrt{\frac{1}{2} \left( 143 + 16\sqrt{79} \right)}} + \sqrt{\frac{1}{2} \left( 141 + 16\sqrt{79} \right)} \\ \gamma \\ \end{cases} \right) \\ \times \\ \gamma \\ \end{cases} \\ \left( 1/15 \right) - (21 + 5) \times \frac{1}{10^3}$$

Result:  $\left(3 + \frac{189}{2}\sqrt{\left(\left(\frac{1}{2}\sqrt{96 + 11\sqrt{79}} + \frac{1}{2}\sqrt{100 + 11\sqrt{79}}\right)\right)} \\ \left(\sqrt{\frac{1}{2}\left(141 + 16\sqrt{79}\right)} + \sqrt{\frac{1}{2}\left(143 + 16\sqrt{79}\right)}\right)\right)^{(1/15)} - \frac{13}{500}$ 

## **Decimal approximation:**

 $1.617813269499360816175543718552125190287489757641818765751\ldots$ 

1.6178132694... result that is a very good approximation to the value of the golden ratio 1,618033988749...

#### **Alternate forms:**

1

$$\begin{split} \overline{500} \\ & \left(250 \times 2^{4/5} \left(3 \left(63 \sqrt{\left(2 \left(2 \sqrt{96 + 11 \sqrt{79}} + 11 \sqrt{2} + \sqrt{158}\right) \left(\sqrt{2 \left(141 + 16 \sqrt{79}\right)} + 8 \sqrt{2} + \sqrt{158}\right) \right)} + 8 \sqrt{2} + \sqrt{158}\right) \left(\sqrt{2 \left(141 + 16 \sqrt{79}\right)} + 8 \sqrt{2} + \sqrt{158}\right) \right) \left(\sqrt{2 \left(141 + 16 \sqrt{79}\right)} + \sqrt{120 + 11 \sqrt{79}}\right) \\ & \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{100 + 11 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{141 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{143 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{143 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{143 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{143 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{79}}\right) \left(\sqrt{143 + 16 \sqrt{79}} + \sqrt{143 + 16 \sqrt{14}}\right) \left(\sqrt{143 + 16 \sqrt{14} + \sqrt$$

Note that all the results of the analyzed Ramanujan expressions, can be connected with the previous solutions obtained from the equations concerning black hole/wormhole physics, that we have previously described.

# **Observations**

*From:* https://www.scientificamerican.com/article/mathematicsramanujan/?fbclid=IwAR2caRXrn\_RpOSvJ1QxWsVLBcJ6KVgd\_Af\_hrmDYBNyU8mpSjRs1BDeremA

Ramanujan's statement concerned the deceptively simple concept of partitions—the different ways in which a whole number can be subdivided into smaller numbers. Ramanujan's original statement, in fact, stemmed from the observation of patterns, such as the fact that p(9) = 30, p(9 + 5) = 135, p(9 + 10) = 490, p(9 + 15) = 1,575 and so on are all divisible by 5. Note that here the n's come at intervals of five units.

Ramanujan posited that this pattern should go on forever, and that similar patterns exist when 5 is replaced by 7 or 11—there are infinite sequences of p(n) that are all divisible by 7 or 11, or, as mathematicians say, in which the "moduli" are 7 or 11.

Then, in nearly oracular tone Ramanujan went on: "There appear to be corresponding properties," he wrote in his 1919 paper, "in which the moduli are powers of 5, 7 or 11...and no simple properties for any moduli involving primes other than these three." (Primes are whole numbers that are only divisible by themselves or by 1.) Thus, for instance, there should be formulas for an infinity of n's separated by  $5^3 = 125$  units, saying that the corresponding p(n)'s should all be divisible by 125. In the past methods developed to understand partitions have later been applied to physics problems such as the theory of the strong nuclear force or the entropy of black holes.

# From Wikipedia

In particle physics, **Yukawa's interaction** or **Yukawa coupling**, named after Hideki Yukawa, is an interaction between a scalar field  $\phi$  and a Dirac field  $\psi$ . The Yukawa interaction can be used to describe the nuclear force between nucleons (which are fermions), mediated by **pions** (which are pseudoscalar mesons). The Yukawa interaction is also used in the Standard Model to describe the coupling between the Higgs field and massless quark and lepton fields (i.e., the fundamental fermion particles). Through spontaneous symmetry breaking, these fermions acquire a mass proportional to the vacuum expectation value of the **Higgs field**.

Can be this the motivation that from the development of the Ramanujan's equations we obtain results very near to the dilaton mass calculated as a type of **Higgs boson**:

**125** GeV for T = 0 and to the Higgs boson mass 125.18 GeV and practically equal to the rest mass of **Pion meson** 139.57 MeV

*Note that:* 

$$g_{22} = \sqrt{(1+\sqrt{2})}.$$

Hence

$$64g_{22}^{24} = e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} - \cdots,$$
  

$$64g_{22}^{-24} = 4096e^{-\pi\sqrt{22}} + \cdots,$$

so that

$$64(g_{22}^{24}+g_{22}^{-24})=e^{\pi\sqrt{22}}-24+4372e^{-\pi\sqrt{22}}+\cdots=64\{(1+\sqrt{2})^{12}+(1-\sqrt{2})^{12}\}.$$

Hence

$$e^{\pi\sqrt{22}} = 2508951.9982\ldots$$

Thence:

 $64g_{22}^{-24} = 4096e^{-\pi\sqrt{22}} + \cdots$ 

And

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1+\sqrt{2})^{12} + (1-\sqrt{2})^{12}\}$$

*That are connected with 64, 128, 256, 512, 1024 and 4096 = 64^2* 

(*Modular equations and approximations to*  $\pi$  - *S. Ramanujan - Quarterly Journal of Mathematics, XLV, 1914, 350 – 372*)

All the results of the most important connections are signed in blue throughout the drafting of the paper. We highlight as in the development of the various equations we use always the constants  $\pi$ ,  $\phi$ ,  $1/\phi$ , the Fibonacci and Lucas numbers, linked to the golden ratio, that play a fundamental role in the development, and therefore, in the final results of the analyzed expressions.

In mathematics, the **Fibonacci numbers**, commonly denoted  $F_n$ , form a sequence, called the **Fibonacci sequence**, such that each number is the sum of the two preceding ones, starting from 0 and 1. Fibonacci numbers are strongly related to the golden ratio: Binet's formula expresses the nth Fibonacci number in terms of n and the golden ratio, and implies that the ratio of two consecutive Fibonacci numbers tends to the golden ratio as n increases.

Fibonacci numbers are also closely related to Lucas numbers, in that the Fibonacci and Lucas numbers form a complementary pair of Lucas sequences

*The beginning of the sequence is thus:* 

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, 233, 377, 610, 987, 1597, 2584, 4181, 6765, 10946, 17711, 28657, 46368, 75025, 121393, 196418, 317811, 514229, 832040, 1346269, 2178309, 3524578, 5702887, 9227465, 14930352, 24157817, 39088169, 63245986, 102334155...

The Lucas numbers or Lucas series are an integer sequence named after the mathematician François Édouard Anatole Lucas (1842–91), who studied both that sequence and the closely related Fibonacci numbers. Lucas numbers and Fibonacci numbers form complementary instances of Lucas sequences.

The Lucas sequence has the same recursive relationship as the Fibonacci sequence, where each term is the sum of the two previous terms, but with different starting values. This produces a sequence where the ratios of successive terms approach the golden ratio, and in fact the terms themselves are roundings of integer powers of the golden ratio.<sup>[1]</sup> The sequence also has a variety of relationships with the Fibonacci numbers, like the fact that adding any two Fibonacci numbers two terms apart in the Fibonacci sequence results in the Lucas number in between.

The sequence of Lucas numbers is:

2, 1, 3, 4, 7, 11, 18, 29, 47, 76, 123, 199, 322, 521, 843, 1364, 2207, 3571, 5778, 9349, 15127, 24476, 39603, 64079, 103682, 167761, 271443, 439204, 710647, 1149851, 1860498, 3010349, 4870847, 7881196, 12752043, 20633239, 33385282, 54018521, 87403803.....

All Fibonacci-like integer sequences appear in shifted form as a row of the Wythoff array; the Fibonacci sequence itself is the first row and the Lucas sequence is the second row. Also like all Fibonacci-like integer sequences, the ratio between two consecutive Lucas numbers converges to the golden ratio.

A Lucas prime is a Lucas number that is prime. The first few Lucas primes are:

2, 3, 7, 11, 29, 47, 199, 521, 2207, 3571, 9349, 3010349, 54018521, 370248451, 6643838879, ... (sequence A005479 in the OEIS).

In geometry, a **golden spiral** is a logarithmic spiral whose growth factor is  $\varphi$ , the golden ratio.<sup>[1]</sup> That is, a golden spiral gets wider (or further from its origin) by a factor of  $\varphi$  for every quarter turn it makes. Approximate logarithmic spirals can occur in nature, for example the arms of spiral galaxies<sup>[3]</sup> - golden spirals are one special case of these logarithmic spirals

We note how the following three values: 137.508 (golden angle), 139.57 (mass of the Pion - meson Pi) and 125.18 (mass of the Higgs boson), are connected to each other. In fact, just add 2 to 137.508 to obtain a result very close to the mass of the Pion and subtract 12 to 137.508 to obtain a result that is also very close to the mass of the Higgs boson. We can therefore hypothesize that it is the golden angle (and the related golden ratio inherent in it) to be a fundamental ingredient both in the structures of the microcosm and in those of the macrocosm.

# References

**Wormholes in generalized hybrid metric-Palatini gravity obeying the matter null energy condition everywhere -** *Joao Luis Rosa, Jose P. S. Lemos, and Francisco S. N. Lobo* - arXiv:1808.08975v1 [gr-qc] 27 Aug 2018,

TRANSACTIONS OF THE AMERICAN MATHEMATICAL SOCIETY Volume 349, Number 6, June 1997, Pages 2125 {2173 S 0002-9947(97)01738-8 **RAMANUJAN'S CLASS INVARIANTS, KRONECKER'S LIMIT FORMULA, AND MODULAR EQUATIONS** -*BRUCE C. BERNDT, HENG HUAT CHAN, AND LIANG - CHENG ZHANG*