# Relation of anomalous magnetic dipole moments of leptons 

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#### Abstract

The relation of anomalous magnetic dipole moments of three charged leptons is assumed.


Key words: Bošković, moment, lepton

## Moments

Let's apply the known dimensionless value: $\boldsymbol{a}=\mathbf{1}(\mathbf{( 2 \pi \alpha})=0,00116140973$
Where $\dot{\boldsymbol{\alpha}}=137.035999084$ is the inverse fine structure constant.
Let us perform the following transformation on the anomalous magnetic dipole moment of the charged leptons to obtain the values, $\boldsymbol{x}_{i}$ :

$$
\begin{equation*}
x_{i}=1 /\left(a / a_{i}-1\right), \quad i=(1,2,3) \tag{1}
\end{equation*}
$$

Where: $\boldsymbol{a}_{\mathbf{i}}$ is the anomalous magnetic dipole moment for the first, second and third generations, i.e.: Electron, Muon and Tau particle, [2]

With intuition and more with understanding [1] we get:

$$
\begin{equation*}
2^{*}\left(x_{2}+x_{3}\right) \approx 1-x_{1} \tag{2}
\end{equation*}
$$

Shown in:

| $i /$ á | Table |  |  |
| :---: | :---: | :---: | :---: |
|  | $a=1 /\left(2 \pi^{*} \dot{\alpha}\right)=$ | 0,001161409733 | moment |
|  | 137,035999084 | $a_{i}$ | $x_{i}=1 /\left(a / a_{i}-1\right)$ |
| 1 | El. 0,00115965218076(27) | 0,00115965218076 | -660,81097442149 |
| 2 | Muon 0,00116592091 (63) | 0,00116592091 | 257,451592677528 |
| 3 | Tau 0,00117721 (5) | 0,00117722 | 73,4538945332408 |
|  |  | $2 *\left(x_{2}+x_{3}\right)-1=$ | 660,81097442154 |

Assuming the accuracy of (2), the least known input data is for Tau, so let's calculate:

$$
\begin{equation*}
x_{3}=\left(1-x_{1}\right) / 2-x_{2} \tag{3}
\end{equation*}
$$

That is, by applying (1) and arranging, we get:

$$
\begin{equation*}
a_{3}=a *\left(1+1 /\left(\left(1-1 /\left(a_{1} / a-1\right)\right) / 2-1 /\left(a_{2} / a-1\right)\right)\right)=0,00117722114 \tag{4}
\end{equation*}
$$

This is probably approximate because we didn't take into account other influences that are most likely from Proton and W boson with a small correction in (2), for example for a proton it is, $\boldsymbol{x}_{\boldsymbol{4}}$ :

| $i$ |  | $a_{i}$ | $\mathrm{x}_{4}=1 /\left(a / a_{\mathrm{i}}-1\right)$ |
| :--- | ---: | ---: | :---: |
| 4 |  | 1,79284735650 | 0,000648222 |

So, when that term is also included in (3), the correction for $\boldsymbol{x}_{3}$ is obtained and then the difference for the value of $\boldsymbol{a}_{3}$ to the tenth decimal place compared to the calculation without proton.

A special symmetry can be seen from the previous formulas, so in (4) we can replace the places with indices 2 and 3 and get:

$$
\begin{equation*}
a_{2}=a *\left(1+1 /\left(\left(1-1 /\left(a_{1} / a-1\right)\right) / 2-1 /\left(a_{3} / a-1\right)\right)\right)=0,00116592091 \tag{5}
\end{equation*}
$$

From this symmetry, we can classify particles differently and say that: we have one member of the primary and two members of the secondary generation.

The transformation, (1) only made the calculation easier: then everything was returned to anomalous magnetic dipole moments.

It is to be expected that a similar transformation can be used for $\boldsymbol{u} \boldsymbol{p}$ types and for down types of quarks for which no measured data are available to me.

## Conclusion

- The ratio of anomalous magnetic dipole moments of three charged leptons was determined, using Ruđer Bošković's Theory.
- Of course, it would be best to use [1] to determine the value for the electron, which I did not do, and which is considered: "the magnetic moment of the electron the most accurately verified prediction in the history of physics", [2], with which I'm not familiar with it.


## References:

[1] Boscovich J. R.: (a) "Theoria philosophia naturalis redacta ad unicam legem virium in natura existentium", first (Wien, 1758) and second (Venetiis, 1763) edition in Latin language; (b) "A Theory of Natural Philosophy", in English, The M.I.T. Press, Massachusetts Institute of Technology, Cambridge, Massachusetts and London, England, first edition 1922, second edition 1966.
[2] https://en.wikipedia.org/wiki/Anomalous_magnetic_dipole_moment

