## A special theory of gravitation

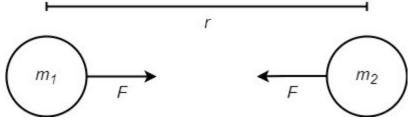
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*Abstract*: Gravitation is relative density of space time caused by mass of object. There are three aspects on gravitation. First related to object. Gravitation can cause changes in velocity and direction of object. Second related to photon, gravitation can change direction and frequency of photon. Third related to difference in the result of observation. Different observers on the same object observation can yield different result. Gravitation cause difference in time period of event, difference in length of object, and difference in mass or energy of object

## 1. INTRODUCTION

According to Newtonian mechanics, gravitation is force of every object attract every other object. The value of gravitational force directly proportional to the product of their mass and inversely proportional to the square of the distance between them.

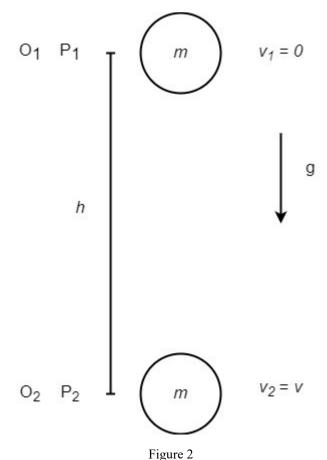




F is force, G is gravitational constant,  $m_1, m_2$  are mass of objects, and r is distance between two objects.

$$F = G \frac{m_1 m_2}{r^2}$$

#### 2. POTENTIAL ENERGY AND KINETIC ENERGY



O<sub>1</sub> is Observer1, O<sub>2</sub> is Observer2 P<sub>1</sub>, P<sub>2</sub> are position 1 and 2 of observers and object. *m*, is mass of object, *V* is velocity of object, and *h* is height between P<sub>1</sub> and P<sub>2</sub>. Object with mass *m* is dropped at position P<sub>1</sub>. Initial velocity *V* is  $V_1 = 0$ . Object then free fall to Position P<sub>2</sub>. At P<sub>2</sub> velocity of object is  $V_2 = V$ 

Object has potential and kinetic energy. Potential energy is energy held by on object because it is at a height. Kinetic energy is form of energy held because of its motion.

$$E_p = mgh$$

 $E_p$  is Potential energy, *m* is mass of object, *g* is gravitation and *h* is height of object.

$$E_k = \frac{1}{2}mv^2$$

 $E_k$  is Kinetic energy, *m* is mass of object *v* is velocity of object.

When an object is dropped from a height there is change in energy from potential energy to kinetic energy.

When position of object is at  $P_1 E_p = mgh$  and  $E_k = 0$  because V = 0.

At position of object is at P<sub>2</sub>  $E_p = 0$  because h = 0 and  $E_k = \frac{1}{2}mv^2$ .

Total energy, potential energy add kinetic energy is constant. There is only changes in forms of energy.

$$mgh_1 + \frac{1}{2}mv_1^2 = mgh_2 + \frac{1}{2}mv_2^2$$

## 3. DIFFERENCE IN TOTAL ENERGY BECAUSE OF DIFFERENCE IN POSITION OF OBSERVER

According to Einstein's special theory of relativity mass equal to energy,  $E = mc^2$ , where E is energy of object, m is mass of object, and c is speed of light. Total energy of object consists of rest mass energy and kinetic energy. When speed of object is much less than speed of light than Newton equation for kinetic energy  $E_k = \frac{1}{2}mv^2$  is still valid.

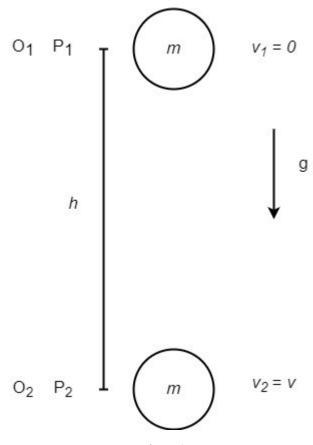


Figure 3

See figure 3

Observer 1 is at position  $P_1$ . Observer 2 at position  $P_2$ .

From the view point of Observer 1 when position of object is at P<sub>1</sub>

h = 0 and v = 0

so

 $E_r = mc^2$ ,  $E_r$  is rest energy  $E_p = mgh$ , because h = 0 then  $E_p = 0$ ,  $E_p$  is potential energy  $E_k = \frac{1}{2}mv^2$ , because v = 0 then  $E_k = 0$ total energy  $= mc^2 + mgh + \frac{1}{2}mv^2 = mc^2$  or  $E_t = E_r$ When position of object is at P2 h = -h and v = v $E_r = mc^2$   $E_p = -mgh,$   $E_k = \frac{1}{2}mv^2$ total energy =  $mc^2 - mgh + \frac{1}{2}mv^2 = mc^2$  or  $E_t = E_r$ because  $mgh = \frac{1}{2}mv^2$ 

From the view point of Observer 2 when position of object is at P1

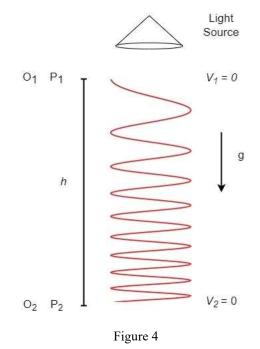
h = h and v = 0  $E_p = mgh,$   $E_k = \frac{1}{2}mv^2 E_k = 0 \text{ because } v = 0$ And total energy  $= mc^2 + mgh + \frac{1}{2}mv^2 = mc^2 + mgh \text{ or } E_t = E_r + E_p$ Because v = 0.
When position of object is at P<sub>2</sub> h = 0 and v = v  $E_p = mgh, E_p = 0$ and  $E_k = \frac{1}{2}mv^2$ and total energy  $= mc^2 + mgh + \frac{1}{2}mv^2 = mc^2 + \frac{1}{2}mv^2$ Because h = 0Or total energy  $E_t = E_r + E_k$ or total energy  $E_t = E_r + E_p$ because  $mgh = \frac{1}{2}mv^2$ 

Observer	Total energy		Difference in total energy
	Position Object at P <sub>1</sub>	Position Object at P <sub>2</sub>	
<b>O</b> <sub>1</sub>	$E_t = E_r$	$E_t = E_r + E_k - E_p = E_r$	No
O <sub>2</sub>	$E_t = E_r + E_p$	$E_t = E_r + E_k$ or $E_t = E_r + E_p$	No
	_	Because $E_k = E_p$	
Difference	Yes	Yes	
in total			
energy			

Table 1

We can see that the cause of difference of total energy is position of the observer, not the position of object

## 4. LIGHT AND GRAVITATION



When light is directed from position  $P_1$  to  $P_2$  then there is change in frequency of light. Observer  $O_2$  at position  $P_2$  will detect the frequency of light higher than the frequency detected by Observer  $O_1$  at position  $P_1$ 

From the viewpoint of Observer O<sub>1</sub> at position P<sub>1</sub>

 $v = v_{1}$   $T_{1} = \frac{1}{v_{1}}$   $\lambda_{1} = \frac{c}{v_{1}}$   $E_{1} = hv_{1}$ 

From the viewpoint of Observer O<sub>2</sub> at position P<sub>2</sub>

$$v = v_{2}$$

$$T_{2} = \frac{1}{v_{2}}$$

$$\lambda_{2} = \frac{c}{v_{2}}$$

$$E_{2} = hv_{2}$$

$$v_{1} < v_{2}, \lambda_{1} > \lambda_{2}, T_{1} > T_{2}, \text{ and } E_{1} < E_{2}$$

$$v \text{ is light frequency.}$$

h is Planck constant

 $\lambda$  is light wavelength

*T* is wave period of light

Compared to Observer 1 at position 1 Observer 2 at position 2 get time is slower, length is shorter and energy is higher.

Observer	Wavelength	Frequency	Period	Energy
O1	$\lambda_1$	$v_{I}$	$T_{I}$	$E_1 = hv_1$
O <sub>2</sub>	$\lambda_2$	$v_2$	$T_2$	$E_2 = hv_2$
Comparison	$\lambda_1 > \lambda_2$	$v_1 < v_2$	$T_1 > T_2$	$E_1 < E_2$
	Table 2			

Note that the light observed by Observer1 and Observer2 is the same light and the same source. The difference in wavelength, frequency
and period are because of difference in position of observers.

## 5. GRAVITATION AS RELATIVE DENSITY OF SPACE TIME

There are three aspects on gravitation. First related to object. Gravitation can cause changes in velocity and direction of object. Second related to photon, gravitation can change direction and frequency of photon. Third related to difference in the result of observation. Different observers on the same object observation can yield different result. Gravitation cause difference in time period of event, difference in length of object, and difference in mass or energy of object.

From section 3 and 4 we see that there are difference in total energy of object and difference in wavelength, frequency, period, and energy of photon. The differences are because of difference in position of observers. I introduce gravitation d as relative density of space time. Value of d is ratio of total energy of an object observed from different position. The value of d is relative. Closer the position of observer to a high mass object then higher the value d. Figure 8 is visualisation of relative density of space time d. Darker the colour means higher the value of relative density of space time d. Closer the position to the high mass object darker the colour.

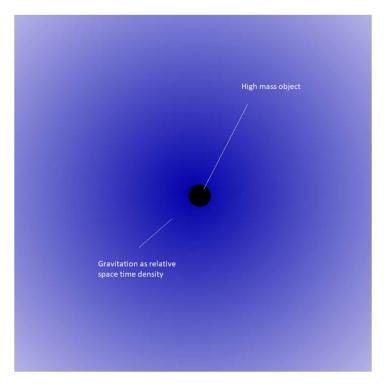


Figure 5

 $d_{relative \ at \ position \ 1 \ to \ position \ 2} = rac{1}{d_{relative \ at \ position \ 2 \ to \ position \ 1}}$ 

Or 
$$d_{12} = \frac{1}{d_{21}}$$
  
And  $d_{21} = \frac{1}{d_{12}}$   
And  $d_{11} = d_{22} = 1$   
 $0 \le d \le \infty$ 

Let observer 1 at position 1 and observer 2 at position 2 and d as relative total energy

$$d_{12} = \frac{E_{total \ observed \ by \ observer \ 1}}{E_{total \ observerd \ by \ observer \ 2}}$$

Or 
$$d_{12} = \frac{E_{t1}}{E_{t2}}$$

And because mass equal to energy,  $E = mc^2$ 

$$d_{12} = \frac{m_1}{m_2}$$

d as relative time interval

$$d_{12} = \frac{t_{time interval observerd by observer 2}}{t_{time interval observed by observer 1}}$$
  
Or  $d_{12} = \frac{t_2}{t_1}$ 

d as relative length

$$d_{12} = \frac{l_{length of object observed by observer 2}}{l_{lengt} of object observer by observer 1}$$
  
Or  $d_{12} = \frac{l_2}{l_1}$ 

## 6. RELATIVE DENSITY OF SPACE TIME FROM MERCURY PLANET TO EARTH.

Relative density d of space time from Mercury planet to Earth is

$$d_{mercury\ ear} = \frac{E_{total\ observed\ by\ observer\ from\ Mercury\ Planet}}{E_{total\ observer\ d\ by\ observer\ from\ Eart}}$$

or

 $d_{me} = \frac{E_{tm}}{E_{te}}$ 

 $E_{te} = mc^2$  $E_{tm} = mc^2 + E_{p (from earth to mercury)}$ 

$$\begin{split} E_p &= \int_{rm}^{re} \frac{GMm}{r^2} dr \\ E_p &= -\frac{GMm}{r} \mid \frac{r_e}{r_m} \\ E_p &= -\left(\frac{GMm}{r_e} - \frac{GMm}{r_m}\right) \\ E_p &= \frac{GMm}{r_m} - \frac{GMm}{r_e} \\ E_p &= GMm \left(\frac{1}{r_m} - \frac{1}{r_e}\right) \\ E_p &= GMm \left(\frac{r_e - r_m}{r_e r_m}\right) \\ d_{me} &= \frac{E_{tm}}{E_{te}} \\ d_{me} &= \frac{E_{te} + E_p}{E_{te}} \\ d_{me} &= \frac{mc^2 + GMm \left(\frac{r_e - r_m}{r_e r_m}\right)}{mc^2} \\ d_{me} &= \frac{c^2 + GM \left(\frac{r_e - r_m}{r_e r_m}\right)}{c^2} \\ d_{me} &= 1 + \frac{GM(r_e - r_m)}{r_e r_m c^2} \\ G &= 6.67384 \ge 10^{-11} m^3 kg^{-1} s^{-2} \\ M &= 1.98847 \ge 10^{30} kg \end{split}$$

- $r_m = 5.74 \ge 10^{10} \text{ m or } 0.574 \ge 10^{11} \text{ m}$
- $r_e = 1.496 \text{ x} 10^{11} \text{ m or } 14.496 \text{ x} 10^{10} \text{ m}$

 $c = 3 \ge 10^8 \ ms^{-1}$ 

$$d_{me} = 1 + \frac{6.67384 \ge 10^{-11} \ 1.98847 \ge 10^{30} (1.496 \ge 10^{11} - \ 0.574 \ge 10^{11})}{1.496 \ge 10^{11} \ge 5.74 \ge 10^{10} \ge 9 \ge 10^{16}}$$

$$d_{me} = 1 + \frac{12.2356136 \times 10^{30}}{77.28336 \times 10^{37}}$$

 $d_{me} = 1 + 1.58321 \ge 10^{-8}$ 

Object of observations	Result from Earth	Calculation from Mercury	Calculation result from Mercury
Mass of the sun	1.98847 x 10 <sup>30</sup> kg	$(1 + 1.58321 \text{ x } 10^{-8}) \text{ x}$ 1.98847 x 10 <sup>30</sup>	1.98847 x 10 <sup>30</sup> kg + 3.14817 x 10 <sup>22</sup> kg

Distance from mercury to	5.79 x 10 <sup>10</sup> m	5.79 x 10 <sup>10</sup>	5.79 x 10 <sup>10</sup> .m – 366 m
the sun		$\overline{1 + 1.58321 \times 10^{-8}}$	
Diameter of the sun	1.3927 x 10 <sup>9</sup> .m	1.3927 x 10 <sup>9</sup>	1.3927 x 10 <sup>9</sup> .m - 22.05 m
		$\overline{1+1.58321 \times 10^{-8}}$	
Average rotating the sun	27 days =	2.3328 x 10 <sup>6</sup>	27 days – 0.036 s
on axis	2.3328 x 10 <sup>6</sup> s	$\overline{1 + 1.58321 \times 10^{-8}}$	
Mass of the universe	1.73 x 10 <sup>53</sup> kg	$(1 + 1.58321 \times 10^{-8}) \times 10^{-8}$	$1.73 \text{ x } 10^{53} \text{kg} +$
		$1.73 \times 10^{53}$	2.739 x 10 <sup>45</sup> kg
Diameter of the universe	93.016 x 10 <sup>9</sup> light	93.016 x 10 <sup>9</sup>	93.016 x 10 <sup>9</sup> light years –
	years	$1 + 1.58321 \times 10^{-8}$	1472.64 light years
		Table 2	

Table 3

#### 7. RELATIVE UNIVERSE

From table 3 we can conclude that observation of mass, length, and rotation period of an object differ between from earth and from mercury. There are so many places in the universe. Value of relative density of space time are different from one place to another places so mass, length, and period of an object differ between them. The result is there are no absolute value of mass, length, and period of time of object in the universe. There are only relative value of mass, length, and period of time. Value mass and diameter of universe are relative value observed from earth, there are so many places outside earth with relative value of d lower than 1, as location far from star at the edge of aur galaxy, or value of d much larger than 1 as at location at the neutron star.

## 8. LOCALISATION PRINCIPLE

Observer O<sub>1</sub> and Observer O<sub>2</sub> at different Position, O<sub>1</sub> at Position P<sub>1</sub> and O<sub>2</sub> at Position P<sub>2</sub>. Relative density  $d_{12} \neq 1$ . They are observed same object. Carbon-12 atomic mass, quartz crystal vibration, and hydrogen atom Bohr radius.:

Observer1 result:

Carbon-12 atomic mass = 12 amu (atomic mass unit)

Quartz crystal vibrate at 32768 times each second

Hydrogen Bohr radius = 1.00054 Å (Ångström)

Observer2 result:

Carbon-12 atomic mass = 12 amu

Quartz crystal vibrate at 32768 times each second

Hydrogen Bohr radius = 1.00054 Å

Both Observer1 and observer2 have the same result when they observe object at the same position with the object.

But if observer1 observes object at position2 the results are

Carbon-12 atomic mass =  $d_{12}x$  12 amu

Quartz crystal vibrate at  $d_{12} \ge 32768$  times each second

Hydrogen Bohr radius =  $\frac{1}{d_{21}} \ge 1.00054$  Å

#### 9. PSEUDO MOVEMENT

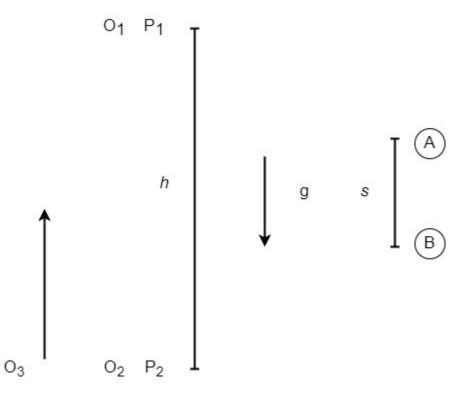


Figure 6

Observer1 stay still at position  $P_1$ , observer2 stay still at position  $P_2$  and observer3 move from position  $P_2$  to position  $P_1$ . Object A and object B is not move.

Observer 1 sees distance from A to B is  $S_1$ 

Observer 2 sees distance from A to B is  $S_2 = \frac{1}{d_{21}} S_1$ 

$$S_1 > S_2$$
,  $\Delta S = S_1 - S_2$ 

When observer3 at position  $P_2$  he saw distance of A to B is  $S_2$ . When Observer 3 arrives at Position  $P_1$  he saw distance of A to B is  $S_1$  then observer 3 sees the pseudo movement between A to B as  $\Delta S$ .

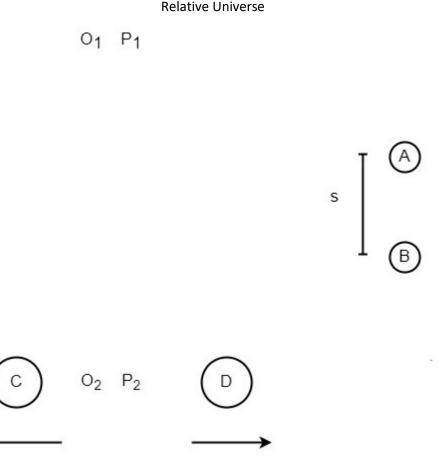


Figure 7

Observer  $O_1$  stay still at position  $P_1$ , observer  $O_2$  stay still at position  $P_2$ . Object A and object B is not move. There are two object C and D move away from O2.

From viewpoint of Observer O1

.

Because there is no change about gravitation at Observer O1 then there is no change in relative density

$$d_{after \ before} = d_{ab} = 1$$

$$S_{1aft} = \frac{1}{d_{ab}} S_{1before}$$

$$S_{1aft} = S_{1befo}$$

.

 $S_{1befo}$  = distance of object A and object B before object C and object D move away from observer O<sub>2</sub>.  $S_{1afte}$  = distance of object A and object B after object C and object D move away from observer O<sub>2</sub>. From viewpoint of Observer O<sub>2</sub>

Because change in distance of object C and D to P2 then relative density at position P2 change.

 $d_{after \ before} = d_{ab} < 1$  $S_{2after} = \frac{1}{d_{ab}} \ S_{2before}$   $S_{2afte} > S_{2before}$ 

 $\Delta S_2 = S_{2aft} - S_{2befo}$ 

 $S_{2before}$  = distance of object A and object B before object C and object D move away from observer O<sub>2</sub>.

 $S_{2af}$  = distance of object A and object B after object C and object D move away from observer O<sub>2</sub>.

Observer  $O_2$  saw there is pseudo movement with value  $\Delta S_2$ . Different with result from Observer  $O_1$  that there is no change in distance of object A and object B

## 10. EXPANDING UNIVERSE

Since the big bang, our universe is continue expanding. Every galaxies move away each other. According to section 9 relative density caused by object move away from observer  $d_{after \ before} = d_{ab} < 1$ .

 $d_{ab} < 1$  cause pseudo movement.

 $v_o = v_r + v_p$ 

 $v_o$  = Velocity of expanding universe seen by observer.

 $v_r$  = Real velocity of expanding universe.

 $v_p$  = Pseudo velocity of expanding <u>universe</u>.

Pseudo movement is part of total velocity of expanding universe seen by observer. Pseudo movement make total velocity of expanding faster than it should.

#### REFERENCES

[1.] Crowell, Benjamin, Mechanics, Light and Matter Fullerton, California, (2019).

[2.] Einstein, Albert, Relativity the special and general theory, Henry Holt and Company, New York, (1920)